

## ON THE INTERMEDIATE-REDSHIFT CENTRAL STELLAR MASS–HALO MASS RELATION, AND IMPLICATIONS FOR THE EVOLUTION OF THE MOST MASSIVE GALAXIES SINCE $z \sim 1$

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Received 2014 August 21; accepted 2014 November 9; published 2014 December 9

### ABSTRACT

The stellar mass–halo mass relation is a key constraint in all semi-analytic, numerical, and semi-empirical models of galaxy formation and evolution. However, its exact shape and redshift dependence remain under debate. Several recent works support a relation in the local universe steeper than previously thought. Based on comparisons with a variety of data on massive central galaxies, we show that this steepening holds up to  $z \sim 1$  for stellar masses  $M_{\text{star}} \gtrsim 2 \times 10^{11} M_{\odot}$ . Specifically, we find significant evidence for a high-mass end slope of  $\beta \gtrsim 0.35\text{--}0.70$  instead of the usual  $\beta \lesssim 0.20\text{--}0.30$  reported by a number of previous results. When including the independent constraints from the recent Baryon Oscillation Spectroscopic Survey clustering measurements, the data, independent of any systematic errors in stellar masses, tend to favor a model with a very small scatter ( $\lesssim 0.15$  dex) in stellar mass at fixed halo mass, in the redshift range  $z < 0.8$  and for  $M_{\text{star}} > 3 \times 10^{11} M_{\odot}$ , suggesting a close connection between massive galaxies and host halos even at relatively recent epochs. We discuss the implications of our results with respect to the evolution of the most massive galaxies since  $z \sim 1$ .

*Key words:* cosmology: theory – galaxies: evolution – galaxies: statistics

*Online-only material:* color figures

### 1. INTRODUCTION

Probing the exact relation between stellar mass and host halo mass is one of the hottest topics in present-day cosmology (Leauthaud et al. 2012; Yang et al. 2012; Behroozi et al. 2013; Moster et al. 2013; Reddick et al. 2013). Such mapping can possibly shed light on the complex and still poorly understood physical processes that govern galaxy evolution (e.g., Silk et al. 2013), as well as unveil key properties of the underlying dark matter cosmological model (e.g., Weinberg et al. 2013).

Constraining the statistical and environmental evolution of massive galaxies, especially those of  $M_{\text{star}} \gtrsim (2\text{--}3) \times 10^{11} M_{\odot}$ , is particularly meaningful. A number of independent observations show that galaxies above this mass scale tend to depart from simple extrapolations of the scaling relations characterizing their lower-mass counterparts, having larger sizes, more prolate shapes, and redder colors (e.g., van der Wel et al. 2009; Bernardi et al. 2011a).

However, the galaxy–halo mapping for massive galaxies as inferred from abundance matching between the stellar and halo mass functions is still under debate. One of the main uncertainties relies on a proper determination of the stellar mass function (e.g., Bernardi et al. 2013; Muzzin et al. 2013). For example, the constant number density evolution of the massive galaxies derived by, e.g., Carollo et al. (2013) at  $z \lesssim 1$  is in disagreement with other measurements at similar redshifts (Maraston et al. 2013; Muzzin et al. 2013).

In this Letter, we provide additional key constraints to the  $M_{\text{star}}\text{--}M_{\text{halo}}$  relation for massive central galaxies at  $0 < z < 1$  using direct stellar and host halo mass measurements of the brightest cluster galaxies (BCGs), as well as accurate galaxy clustering measurements at  $0.4 < z < 0.8$ . The galaxy clustering measurements are used to infer the host halo mass distributions through the halo occupation distribution (HOD) models (e.g., Zheng et al. 2007), and thus provide a powerful tool to break the degeneracies inherent to the abundance matching techniques.

In the following, we will adopt a cosmology with parameters  $\Omega_m = 0.30$ ,  $\Omega_b = 0.045$ ,  $h = 0.70$ ,  $\Omega_\Lambda = 0.70$ ,  $n_s = 1$ , and  $\sigma_8 = 0.8$  to match the one assumed in our reference stellar mass functions and halo occupation measurements. We will adopt the Chabrier initial mass function (IMF; Chabrier 2003) as a reference.

## 2. METHOD

To provide constraints on the galaxy–halo mapping at  $z > 0$ , we evaluate the median stellar mass at fixed host halo mass by direct abundance matching between the stellar and halo mass functions at a given redshift,

$$\Phi(>M_{\text{star}}, z) = \Phi_c(>M_{200c}, z) + \Phi_s(>M_{200c}, z), \quad (1)$$

with  $M_{200c}$  the halo masses defined as 200 times the critical density at redshift  $z$ . The  $\Phi_c(>M_{200c}, z)$  term refers to the host halo mass function, which we take from Tinker et al. (2008), as it can be adapted to diverse halo definitions, and it is well defined up to  $M_{200c} \lesssim 10^{15} M_\odot$ . Equation (1) includes the subhalo term  $\Phi_s(>M_{200c}, z)$  with unstripped mass  $M_{200c}$ , which we take from Behroozi et al. (2013). Neglecting the satellite term in Equation (1) makes very little difference in the halo mass range of interest here, e.g.,  $M_{200c} \gtrsim 10^{13} M_\odot$ .

It is instead much more relevant to adopt the proper intrinsic scatter  $\Sigma$  in stellar mass at fixed halo mass, ideally constrained from independent data sets, as larger values of  $\Sigma$  induce a flatter  $M_{\text{star}}-M_{\text{halo}}$  relation above the break. Equation (1) does not assume any scatter between stellar and halo mass; however, one straightforward way to include it is as follows (see also, e.g., Behroozi et al. 2010). At any redshift of interest, we first fit the parameters of a two power-law relation defined as

$$M_{\text{star}} = M_{\text{star}}^0 \left( \frac{M_{200c}}{M_{200c}^0} \right)^\alpha \left[ 1 + \left( \frac{M_{200c}}{M_{200c}^0} \right)^\gamma \right]^{-1} \quad (2)$$

to the raw output of Equation (1). We then choose a value for the intrinsic scatter  $\Sigma$ , and generate a large galaxy catalog by assigning to each (sub)halo extracted from the total halo mass function a galaxy with stellar mass derived from a Gaussian distribution with a mean given by the logarithm of Equation (2), and dispersion  $\Sigma$  (in dex). We finally vary  $\gamma$  in Equation (2) to tune the high-mass end slope  $\beta = \alpha - \gamma$  until the input stellar mass function in Equation (1) is fully reproduced.

## 3. DATA

The data on BCGs in groups and clusters considered in this Letter are derived at  $z = 0.1$  from X-rays (Kravtsov et al. 2014), at  $0.2 < z < 1$  from X-ray and weak lensing in COSMOS (Finoguenov et al. 2007; George et al. 2011; Huertas-Company et al. 2013a), at  $0.8 < z < 1.4$  from IR (SpARCS; Lidman et al. 2012; van der Burg et al. 2013) and X-ray data (Strazzullo et al. 2010; Raichoor et al. 2011; Rettura et al. 2011), and at  $z \sim 1$  from the Cl1604 supercluster and other structures from the ORELSE survey (Ascaso et al. 2014). Masses are either virial masses or defined to be 200 times the critical density of the universe at the redshift of interest.

As for clustering, we utilize the massive galaxies at the median redshift of  $z \sim 0.6$  from the CMASS sample of the Sloan Digital Sky Survey-III (SDSS-III) Baryon Oscillation Spectroscopic Survey (BOSS; Dawson et al. 2013). Stellar masses are from the Portsmouth spectral energy distribution

fitting (Maraston et al. 2013), originally derived assuming a Kroupa IMF (Kroupa 2001). The host halo masses for these massive galaxies are estimated through the HOD modeling of the projected-space two-point correlation functions on scales from  $0.1 h^{-1} \text{Mpc}$  to  $60 h^{-1} \text{Mpc}$ , faithfully following the method laid out in Guo et al. (2014).

## 4. RESULTS

### 4.1. The Number Density of Massive Galaxies

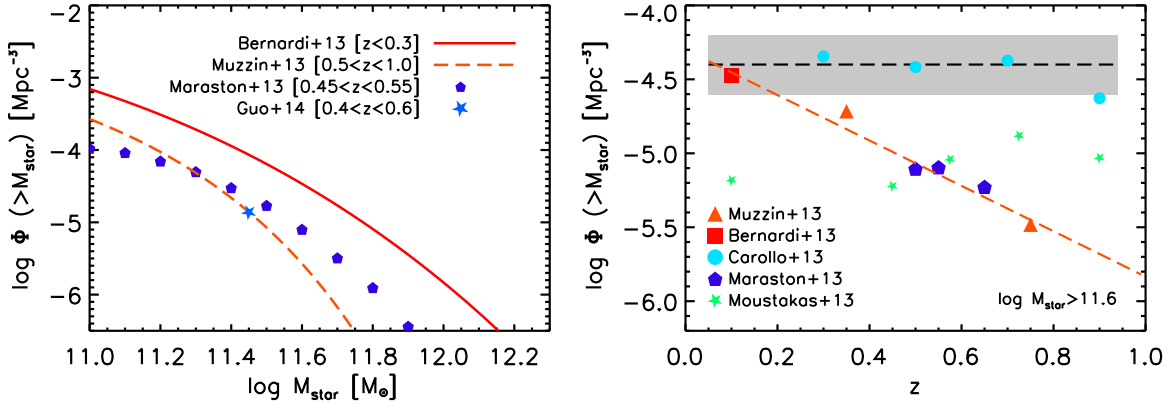
The first step toward defining a more secure mapping between stars and halos relies on properly measuring the stellar mass function of galaxies. The left panel of Figure 1 shows the cumulative number density of galaxies from Bernardi et al. (2013) for the SDSS Data Release 7 main galaxy sample ( $z \lesssim 0.2$ ; solid red line). We used their estimate based on Sérsic-exponential light profile, which is considered by the authors to be the most realistic one to describe SDSS data (Bernardi et al. 2014). When compared to the COSMOS/UltraVISTA data by Muzzin et al. (2013; long-dashed line), at the average redshift of  $z = 0.75$ , or the BOSS estimate from Guo et al. (2014; star), or even the BOSS determination of the stellar mass function by Maraston et al. (2013; diamonds), it would imply at face value a significant increase in the number density of massive galaxies toward low redshifts.

The right panel of Figure 1 focuses on the number density evolution of galaxies above  $M_{\text{star}} \gtrsim 4 \times 10^{11} M_\odot$ . For completeness, this panel also reports the measurements inferred by Moustakas et al. (2013) and Carollo et al. (2013), which would instead suggest a negligible evolution since  $z \lesssim 1$ . Moustakas et al. (2013) is well consistent with the stellar mass function by Maraston et al. (2013). Carollo et al. (2013) do not subtract stellar mass losses from the total masses, thus explaining at least part of the inconsistency with other determinations.

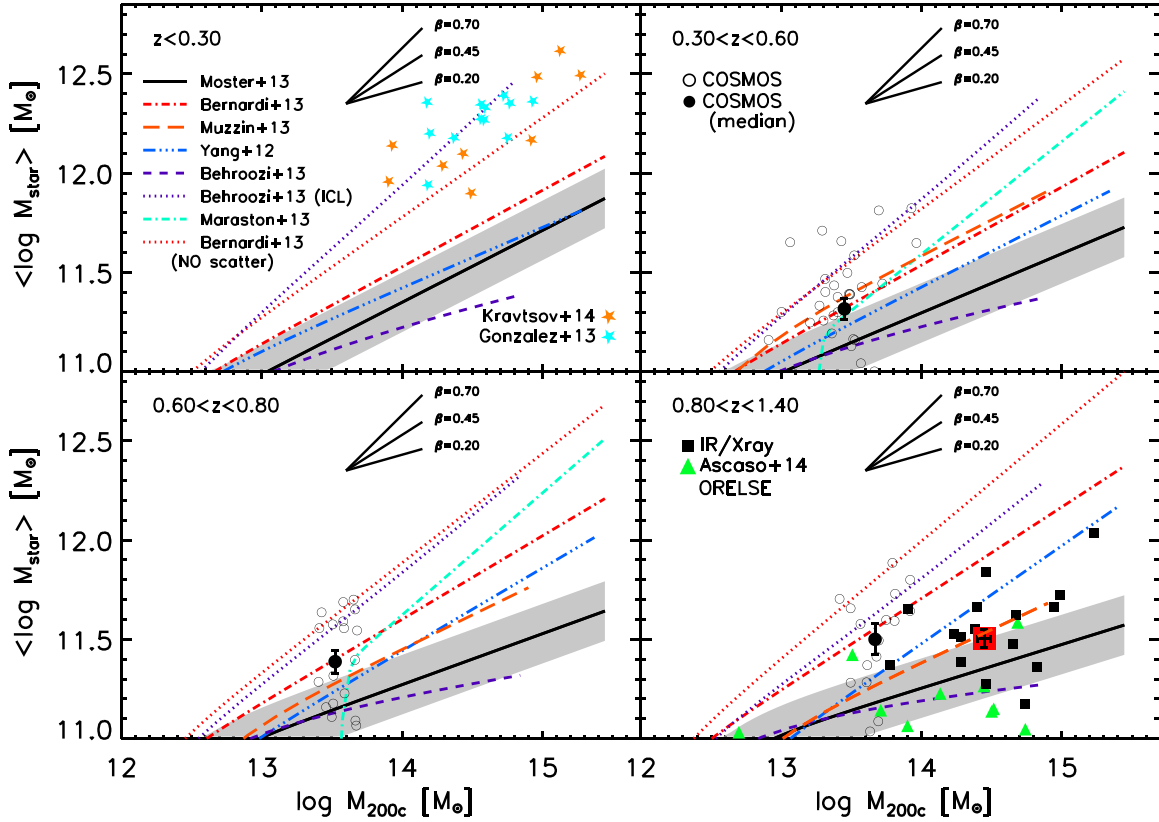
Overall, the right panel of Figure 1 brackets the possible evolutionary paths since  $z \lesssim 1.0$  for the number density of massive galaxies, from a non-evolving scenario (black long-dashed line), to a fast evolving one (orange dashed line). The most relevant measurements broadly fall within these sequences (e.g., Ilbert et al. 2013). The exact determination of the evolution and normalization of the high-mass end of the stellar mass function is limited by photometric and spectral systematics in the determination of stellar masses, as well as possible incompleteness and/or cosmic variance issues (e.g., Marchesini et al. 2009; Bernardi et al. 2010, 2013; Ilbert et al. 2013; Muzzin et al. 2013). In the following, we will evaluate the stellar mass–halo mass relation considering both of these extreme cases, and, by direct comparison with independent data sets, namely, large-scale clustering, set constraints on plausible evolutionary paths for the most massive galaxies in light of current estimates of the stellar mass function.

### 4.2. The Stellar Mass–Halo Mass Relation

Figure 2 shows the median stellar mass as a function of host halo mass for central galaxies evaluated at  $z = 0.1$  (upper left),  $z = 0.4$  (upper right),  $z = 0.7$  (lower left), and  $z = 1.1$  (lower right) for different models. All halo masses in this figure have been defined as 200 times the critical density at the redshift of observation. The dot-dashed red lines are obtained by inserting into Equation (1) the Bernardi et al. (2013) stellar mass function, assumed to be constant up to  $z \sim 1$ , and inclusive of a scatter of  $\Sigma = 0.25$  dex in stellar mass at



**Figure 1.** Left: comparison among different cumulative stellar mass functions in the recent literature at different redshifts, as labeled. Right: redshift evolution of the cumulative number density of galaxies with  $M_{\text{star}} \gtrsim 4 \times 10^{11} M_{\odot}$ . The data by Bernardi et al. (2013; square) and Carollo et al. (2013; circles) would suggest at face value a negligible evolution in the cumulative number density, at least up to  $z \lesssim 0.8$ , but not so when considering other data. Where needed, we converted from a Kroupa (2001) to a Chabrier (2003) IMF via a constant shift of  $-0.05$  dex (e.g., Bernardi et al. 2010), and corrected for the (usually small) differences in cosmology. (A color version of this figure is available in the online journal.)



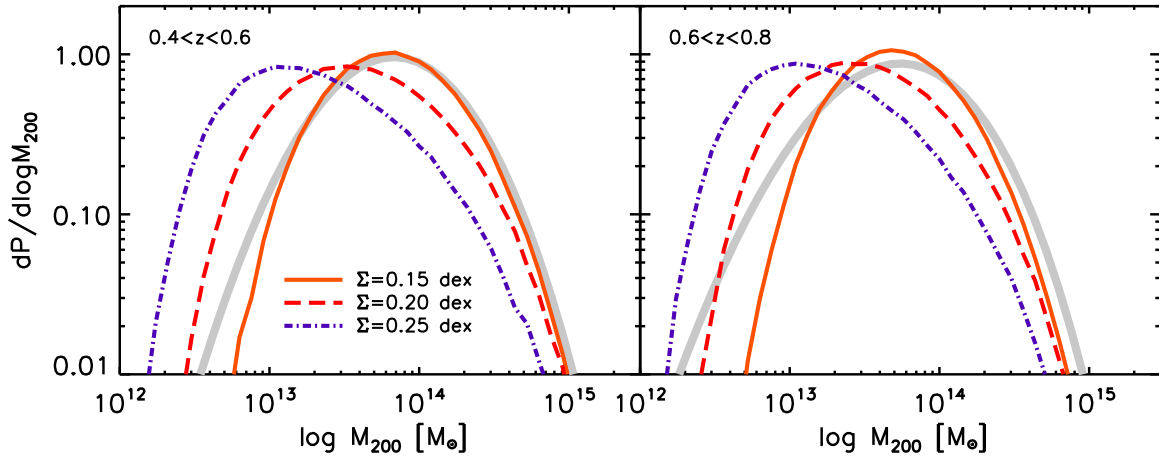
**Figure 2.** Median stellar mass as a function of halo mass relation for central galaxies at  $z = 0.1, 0.4, 0.7, 1.1$ , clockwise from the upper left panel, respectively. The red dot-dashed and red dotted lines are derived from the Bernardi et al. (2013) stellar mass function, assumed constant at all redshifts above  $M_{\text{star}} \gtrsim 10^{11} M_{\odot}$ , with an intrinsic scatter of  $\Sigma = 0.25$  and  $\Sigma = 0$  dex, respectively. The solid line and gray area mark the Moster et al. (2013) median relation and its  $1\sigma$  uncertainty region, respectively. The blue dashed line is the result by Yang et al. (2012). All the data are as labeled. The filled circles mark the median stellar mass–halo mass in the COSMOS data, while the red square the median in the IR/X-ray plus Ascaso et al. (2014) and other associated data. (A color version of this figure is available in the online journal.)

fixed halo mass. The dotted lines refer to the same model but without scatter.

The long-dashed orange lines instead adopt the Muzzin et al. (2013) stellar mass function, only valid at  $z > 0.2$ , with an intrinsic scatter of  $\Sigma = 0.15$  dex. For completeness, we compare these results with three mappings from the recent literature, the Moster et al. (2013) median relation (solid black lines), with its  $1\sigma$  error bar (gray area), the Yang et al. (2012) relation

(dot-dashed blue lines), and the Behroozi et al. (2013) model (dashed purple lines). Other recent works mostly lie within the Moster et al. (2013) uncertainty region (e.g., Leauthaud et al. 2012). For completeness, we also show with purple dotted lines, the Behroozi et al. (2013) model inclusive of the total intra-cluster light.

Overall, most of the recent estimates of the stellar mass–halo mass relation tend to be discrepant with respect to direct central



**Figure 3.** Predicted halo mass distributions from the three mapping of interests in this Letter, as labeled, compared to the BOSS clustering data from Guo et al. (2014) at  $z = 0.5$  (left) and  $z = 0.7$  (right). Models with too large intrinsic scatter in stellar mass at fixed halo mass are challenged by the BOSS data.

(A color version of this figure is available in the online journal.)

galaxy mass measurements in groups and clusters. All the available data collected in this work, in fact, although with a large dispersion, tend to lie, on average, above the Moster et al. (2013) uncertainty region, implying a steeper stellar mass–halo mass relation, with the high-mass end slope (Equation (2)) increasing from  $\beta \lesssim 0.2\text{--}0.3$  to  $\beta \gtrsim 0.35\text{--}0.70$ . Such a discrepancy was already emphasized at  $z < 0.3$  by some groups (e.g., Kravtsov et al. 2014; Shankar et al. 2014). Kravtsov et al. (2014), in particular, recomputed abundance matching with the Bernardi et al. (2013) stellar mass function, finding a steeper relation above  $M_{\text{star}} \gtrsim 10^{11} M_{\odot}$ , broadly consistent with their direct nine BCG stellar and halo mass measurements (orange stars). Our own determinations of the stellar mass–halo mass relation via Equation (1) based on the local Bernardi et al. (2013) stellar mass function without scatter (red dotted lines in Figure 2) are at  $z = 0.1$  broadly consistent with the Kravtsov et al. (2014) and Gonzalez et al. (2013) data at very high masses.

One of the primary causes of the discrepancies can be ascribed to the adoption of different input stellar mass functions. In particular, the Bernardi et al. (2013) stellar mass function, based on improved sky subtractions and modeling of the central galaxy light profile, is characterized by a significant boost in the abundance of the most massive galaxies, which in turn induces a steepening of the stellar mass–halo mass relation. Other factors contribute to the differences in Figure 2. Moster et al. (2013), for example, took care in de-convolving their adopted stellar mass function by some systematic errors before applying Equation (1), thus producing a flattening in the high-mass end of their inferred stellar mass–halo mass relation.

#### 4.3. Independent Constraints from Clustering

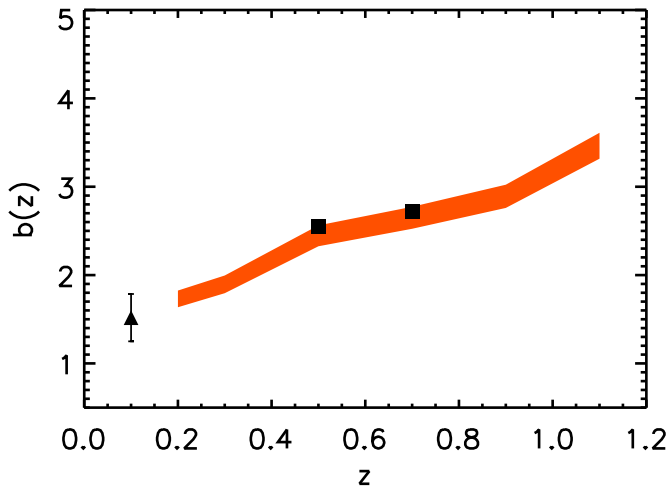
Figure 2 also reveals that at  $z \sim 0.3\text{--}0.6$ , a clear degeneracy exists between a model based on Muzzin et al. (2013), with an intrinsic scatter in stellar mass at a fixed halo mass of  $\Sigma = 0.15$  dex (long-dashed orange lines), and the one based on the  $z = 0.1$  Bernardi et al. (2013) stellar mass function with  $\Sigma = 0.25$  dex (dot-dashed red lines). In fact, both models can potentially reproduce the COSMOS data, though the latter with larger scatter would imply a constant number density at least up to  $z \sim 0.8$ , at variance with the former. Irrespective of uncertainties on stellar masses, we discuss in this section how to use clustering to set a secure upper limit to  $\Sigma$ .

Figure 3 displays with gray bands the Guo et al. (2014) HOD host halo mass distributions for central galaxies<sup>18</sup> with stellar mass above  $\log M_{\text{star}} > 11.50$  (Kroupa IMF) at  $z = 0.5$  (left) and  $z = 0.7$  (right) inferred from the BOSS CMASS clustering measurements (Section 3). For the stellar mass of interest here, the galaxy sample is almost complete and the tiny fraction of missing galaxies due to the CMASS sample selections has negligible effects on the clustering measurements (Maraston et al. 2013; Guo et al. 2014). We compare the BOSS results with the abundance matching model based on the Muzzin et al. (2013) stellar mass function, which perfectly matches the cumulative number density adopted by Guo et al. (2014; left panel of Figure 1). At each redshift of interest, we generate a mock halo catalog extracted from the halo mass function, and populate the halos with galaxies through the stellar mass–halo mass relation based on Muzzin et al. (2013) with a given dispersion  $\Sigma$  that matches the mass cut in BOSS.

Our results are shown in Figure 3 for three different values of the scatter  $\Sigma = 0.15, 0.20, 0.25$  dex, as labeled. Consistently with the reference HOD model, all our mock catalogs have halo masses defined as 200 times the background density at the redshift of interest, and matched to the stellar mass cut in BOSS. Models based on scatters larger than  $\Sigma > 0.15$  dex inevitably map galaxies at fixed stellar mass to host halo masses significantly lower than that inferred from clustering measurements. A larger scatter tends to flatten overall the  $M_{\text{star}}\text{--}M_{\text{halo}}$  relation above the break. However, increasing the scatter also includes lower mass, more numerous halos in samples defined by stellar mass thresholds, thus effectively lowering the median halo mass at fixed stellar mass.

The lower scatter of  $\Sigma = 0.15$  dex is fully consistent with the inferred scatter  $\sigma_{\log M_{200}}$  ( $\sim 0.62$  at  $z = 0.5$  and  $\sim 0.76$  at  $z = 0.7$ ) in the HOD model, which describes the scatter in the host halo mass distribution for the stellar mass sample. The scatter  $\sigma_{\log M_{200}}$  can be converted into  $\Sigma$  through  $\Sigma = p \sigma_{\log M_{200}} / \sqrt{2} \sim 0.17$  when assuming a power-law relation of  $M_{\text{star}} \propto M_{200}^p$  (Zheng et al. 2007), with  $p \sim 0.35$  as found for Muzzin et al. (2013; cf. Figure 2). Our results of a low scatter are in line with and extend

<sup>18</sup> Given the numerous complexities and variables at play in properly modeling satellites in abundance matching, e.g., redshift of infall, effect of environment, etc. (e.g., Neistein et al. 2011; Yang et al. 2012), we here discuss predictions for only central galaxies and focus on the large-scale clustering and bias. The fraction of satellites in our stellar mass range is very small (Guo et al. 2014).



**Figure 4.** Median bias as a function of redshift for galaxies above  $M_{\text{star}} \gtrsim 3 \times 10^{11} M_{\odot}$ , as predicted by our reference stellar mass–halo mass mapping. The colored contour defines the systematic uncertainty associated to the Sheth et al. (2001) and Tinker et al. (2005) biases. Data are extracted from the results by Yang et al. (2007; filled triangles) and Guo et al. (2014; filled squares). (A color version of this figure is available in the online journal.)

several previous estimates (e.g., More et al. 2009; Moster et al. 2010; Leauthaud et al. 2012; Yang et al. 2012; Rodriguez-Puebla et al. 2014).

Analogously, the low-scatter model is fully consistent with the predicted large-scale bias as a function of redshift (Figure 4) derived by Guo et al. (2014) from BOSS data (filled squares), all defined for galaxies above  $M_{\text{star}} \gtrsim 3 \times 10^{11} M_{\odot}$ . The colored contour defines the systematic uncertainty associated to the Sheth et al. (2001) and Tinker et al. (2005) biases. For completeness, in the Figure 4, we also report the  $z \sim 0.1$  bias (filled triangle) extracted from the Yang et al. (2007) catalog, and matched to the Bernardi et al. (2014) SDSS revised stellar masses (see also Huertas-Company et al. 2013b and Shankar et al. 2014).

Our result on a low scatter in the stellar–halo mass relation is independent of systematics in stellar masses, at least for central galaxies. In fact, any error in stellar mass will equally propagate in the cumulative number density and connected HOD clustering modeling. Higher stellar masses, for example, will induce larger number densities and proportionally lower, large-scale characteristic correlation lengths (thus lower-median host halo masses) above a fixed limit in stellar mass (Bernardi et al. 2013). Our stellar–halo median relation, based on Equation (2), will also map galaxies to lower host halo masses, but will still require a low scatter  $\Sigma$  to fully match the HOD results.

## 5. DISCUSSION

In this Letter, we found significant evidence for the following.

1. A steeper stellar mass–halo mass relation with  $\beta \gtrsim 0.35$ – $0.70$  instead of  $\beta \lesssim 0.2$ – $0.3$  from previous works.
2. A low scatter  $\Sigma \lesssim 0.15$  dex in stellar mass at fixed host halo mass, at least up to  $z \sim 0.8$ .

Our results can potentially set valuable constraints to the viable evolutionary paths of massive galaxies.

We first take the Bernardi et al. (2013) stellar mass function as the  $z \sim 0$  reference, as it well matches all local data on massive BCGs (upper left panel of Figure 2). A steadily decreasing number density of massive galaxies at  $0.3 < z < 0.8$  (e.g.,

Muzzin et al. 2013, right panel of Figure 1) would then, at face value, be consistent with most of the available constraints on the group and cluster centrals, keeping  $\Sigma \lesssim 0.15$  dex to match the HOD halo mass distributions inferred from the BOSS clustering measurements (Figure 3).

Another extreme case is forcing the Bernardi et al. (2013) number density of massive galaxies to be constant up to  $z \sim 1$  (e.g., Carollo et al. 2013, right panel of Figure 1). However, the latter model, coupled to the need for a negligible scatter  $\Sigma$ , would imply a systematic overestimate of a factor of  $\gtrsim 5$  in the median BCG stellar mass, as currently measured in clusters at  $z \gtrsim 0.8$  for  $\log M_{200c}/M_{\odot} \gtrsim 14.5$  (red dotted line versus red square in the bottom right panel of Figure 2), and an overestimate of a factor  $\sim 2$  of the total stellar plus intra-cluster light model by Behroozi et al. (2013; purple dotted lines in Figure 2).

Irrespective of the systematics in the stellar mass function, current BCG mass determinations and HOD clustering measurements may favor an increase of a factor of a few since  $z \lesssim 1$  in the number density of the most massive galaxies. This can be partly induced by a parallel growth in the median stellar mass. Independent semi-empirical studies indeed suggest an increase in stellar mass by a factor of  $\sim 2$  since  $z \lesssim 1$  (e.g., Zheng et al. 2007; Lidman et al. 2013; Ascaso et al. 2014; Marchesini et al. 2014). As supported by state-of-the-art hierarchical galaxy evolution models (e.g., De Lucia et al. 2006; Shankar et al. 2013), a non-negligible contribution to this mass growth can be explained by minor and major mergers. The latter, in particular, might be the ones responsible for the steepening in the high-mass end of the scaling relations characterizing early-type galaxies (e.g., Bernardi et al. 2011b).

F.S. acknowledges Naresh Shankar, Jeremy Tinker, David Weinberg, Federico Marulli, and Surhud More for several interesting and helpful discussions. V.B. is supported financially by the National Research Foundation of South Africa. D.M. acknowledges the support of the Research Corporation for Science Advancement’s Cottrell Scholarship. This work is based on data obtained with the *Spitzer Space Telescope*, which is operated by the Jet Propulsion Laboratory (JPL), California Institute of Technology (Caltech), under a contract with NASA. We thank the referee for a constructive report that significantly improved the presentation of the results.

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