

1 Investigation of toughness of ultra high performance fibre reinforced  
2 concrete (UHPFRC) beam under impact loading

3 L. Mao<sup>1\*</sup>, S.J. Barnett<sup>2</sup>

4 <sup>1</sup>Department of Aeronautical and Automotive Engineering, Loughborough University, Epinal Way,

5 Loughborough, LE11 3TU, UK

6 <sup>2</sup>School of Civil Engineering and Surveying, University of Portsmouth, Winston Churchill Avenue,

7 Portsmouth, PO1 2UP, UK

8 \* Corresponding author [l.mao@lboro.ac.uk](mailto:l.mao@lboro.ac.uk)

9 **Abstract:**

10 This paper provides a systematic study about toughness of ultra high performance fibre  
11 reinforced concrete (UHPFRC) in order to better understand the UHPFRC resistance under  
12 impact loading condition. UHPFRC beams containing various fibre volumes are tested under  
13 impact load at different strain rate. From the test results, the relationship between UHPFRC  
14 toughness and strain rate can be determined. Moreover, a numerical model of UHPFRC  
15 beam under impact load is developed and its performance is verified using test data. With  
16 developed UHPFRC model, the evolution of UHPFRC toughness can be better investigated.

17 **Keywords:**

18 UHPFRC, toughness, impact load, numerical simulation, strain rate

19 **1 Introduction:**

20 As ultra high performance fibre reinforced concrete (UHPFRC) material has significant higher  
21 strength than the normal strength concrete, it is more commonly used in civil engineering  
22 field, especially applications associated with high strain rate loadings. Therefore, in order to  
23 maximize the advantages of UHPFRC, its properties and performance under these loading  
24 conditions have received much attention in the last few decades.

25 Habel et al. (2006) studied the evolution of UHPFRC properties, including strength, stiffness,  
26 related to hydration. Isaacs et al.(2009) designed novel techniques to perform material  
27 characterization tests on UHPFRC, including compression and tension tests. With these tests,  
28 the compressive and tensile behaviours of UHPFRC could be investigated. Kang et al.(2010),  
29 Kim et al.(2011), and Park et al.(2012) performed several tests to study the tensile  
30 behaviour of UHPFRC with various fibre volumes. Moreover, blast tests were carried out by  
31 Gupta et al.(2007), Ngo et al.(2007), Barnett, S.J.(2008), Yi et al.(2012), Mao et al. (2014,  
32 2015) to investigate performance of UHPFRC, including deflection and crack pattern, under  
33 blast loading.

34 According to previous studies, due to its high strength, UHPFRC can perform better than  
35 conventional concrete material under high strain rate loadings. Moreover, similar to normal  
36 strength concrete material, UHPFRC properties, such as compressive strength, tensile  
37 strength, and elastic modulus, will be increased with strain rate, but dynamic increase factor  
38 (DIF) values of UHPFRC at various strain rates are different to that from normal strength  
39 concrete, which can be found in Millard et al. 2010, where the dynamic increase factors of  
40 tensile and shear strengths at various strain rate values, with a series of tensile and shear  
41 tests on UHPFRC specimen.

42 However, as another important parameter, toughness can represent the energy absorbing  
43 ability of the material, and can be used to determine the resistance to the fracture under  
44 loading condition, but investigation of toughness has received less attention in the past few  
45 years, especially at high rate loading conditions. Barnett (2008) performed tests on UHPFRC  
46 beam with drop hammer method, and indicated the beam toughness would change with  
47 strain rate. Some other investigations have also been performed to UHPFRC specimen to  
48 clarify the relationship between UHPFRC toughness and strain rate (Cotsovos, 2010,  
49 Mechtcherine et al. 2011, Bragov et al. 2013), but the results are still inconclusive and even  
50 contradictory. Therefore, it is necessary to perform a systematic investigation to UHPFRC  
51 specimen, so that the evolution of UHPFRC toughness with strain rate can be better  
52 understood.

53 This paper presents a systematic study to investigate toughness of UHPFRC beam containing  
54 various fibre volumes at different strain rates. In the tests, drop hammer method is used,  
55 that is, hammer is released at different heights to achieve various strain rate values, and  
56 fibreboards are employed to attenuate the hammer load. As the load is measured at beam  
57 supports, it also contain information related to beam vibration, this effect will be  
58 investigated in this study by analysing frequency spectrum of measured support load, and  
59 will be removed with designed filter. With processed support load and beam deflection, the  
60 toughness value could be obtained and relationship between UHPFRC toughness and strain  
61 rate was determined. Moreover, numerical analysis is performed in the study to obtain  
62 UHPFRC toughness at wider range of strain rate. The stress-strain curve of numerical model  
63 is configured to match design stress-strain relationship of UHPFRC, and performance of  
64 developed models is verified by comparing force-deflection relationship with tested UHPFRC

65 beams. With both experimental tests and numerical analysis, the evolution of UHPFRC  
66 toughness with strain rate can be better understood.

## 67 2 Experimental study of UHPFRC beam toughness with strain rate

68 In this section, the mix proportions of tested UHPFRC beams are described, and drop  
69 hammer tests is applied to UHPFRC beams. From tests, support loads and UHPFRC  
70 deflection can be obtained to generate UHPFRC toughness, it should be mentioned that  
71 information contained in measured support load is further investigated, and design filter  
72 will be used to remove beam vibration effect from measured support load. With test data,  
73 UHPFRC beam toughness at various strain rates will be investigated, and relationship  
74 between UHPFRC beam toughness and strain rate can be better understood.

### 75 2.1 Description of UHPFRC beam

76 In the study, the tested UHPFRC beam is manufactured at University of Liverpool, they are  
77 cast horizontally and compacted using a vibrating table. Beams are produced in batches of three  
78 panels. Cube specimens are also manufactured from each batch in order to measure compressive  
79 strength of the concrete and check consistency of the results between batches. After 24 hours, all  
80 specimens are removed from the moulds and transferred to a hot water curing tank set at 90 °C  
81 where they remain until they were 7 days old. Following this hot curing treatment, there is very  
82 little further change in the compressive strength of the concrete. Optimized packing density of  
83 UHPFRC beam is achieved using 10% fine silica fume with typical particle size of 100-500nm,  
84 and 35% ground granulated blast furnace slag (GGBS) is also employed to replace cement in  
85 the concrete to increase its workability. Table 1 lists the detailed mix proportions of UHPFRC  
86 beam used in the tests.

87

Table 1 Mix proportions of UHPFRC beam

Cementitious component ( $kg/m^3$ )				Aggregate Sand ( $kg/m^3$ )	Water- binder ratio	Structuro 1180 superplasticiser
Cement	GGBS	Silica fume	Whole			
657	418	119	1194	1051	0.17	40

88

89 Moreover, short steel fibres are added to UHPFRC beam to enhance its flexural strength.

90 Three kinds of steel fibre combinations are selected in the study, including 2% short steel

91 fibres (13mm in length) by volume, 6% short steel fibres (13mm in length) by volume, and 6%

92 hybrid steel fibres (3% short fibre of 13mm long, and 3% long fibre of 25mm long) by

93 volume. The use of hybrid fibre is to investigate the enhanced post-cracking performance of

94 UHPFRC beam with combination of several steel fibre types.

95 In the manufacturing process, the elevated temperature curing technique is used to the

96 UHPFRC beam, the tested specimens are cured under damp Hessian for 24 hours, then

97 these specimens are conditioned at 90°C in hot water tank for six days.

98 The dimension of tested UHPFRC beam is 350mm×100mm×50mm. In the tests, the beam is

99 simply supported, giving effective beam span of 300mm, and is rotated through 90° so that

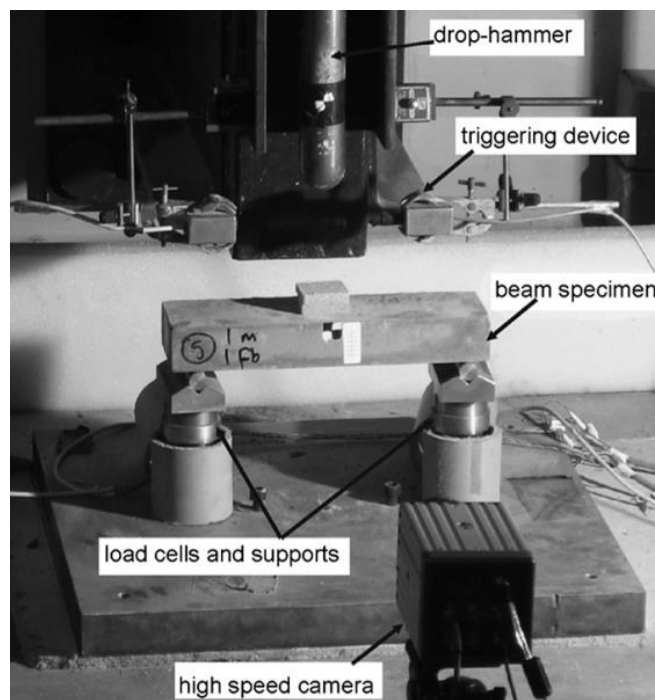
100 its top and bottom surfaces are smooth surfaces.

## 101 2.2 Drop hammer test

102 In the study, the drop hammer technique is used to investigate UHPFRC beam behaviour at

103 various strain rates. The weight of drop hammer is 23.3kg and its maximum release height is

104 2m. Moreover, fibreboard with 10mm thickness is employed in the test. Therefore, strain  
105 rate could be adjusted by using different layers of fibreboards and hammer release heights.  
106 It should be noted that as the applied load from drop hammer can not be measured directly,  
107 the support loads is measured with load cells beneath the roller supports, which is depicted  
108 in Figure 1. It can be seen from figure that load cells are located on a 50mm thick steel base,  
109 which is located on a 10mm layer of fibreboard.



110

111

Figure 1 Drop hammer test

112

113 Moreover, deflection of UHPFRC beam (marked position in Figure 1) is measured in the tests  
114 with high speed camera placed in front of UHPFRC beam, and signal filtering is applied to  
115 reduce the noise level in measured deflections.

116 In this study, the strain rate is calculated using bending beam theory, which has been  
117 adopted for the strain rate calculation in previous studies (Cotsovos, 2010, Millard et al.  
118 2010), the measured deflection is used to calculate the maximum strain in the beam, and  
119 then maximum strain rate is obtained by differentiating strain with respect of time.

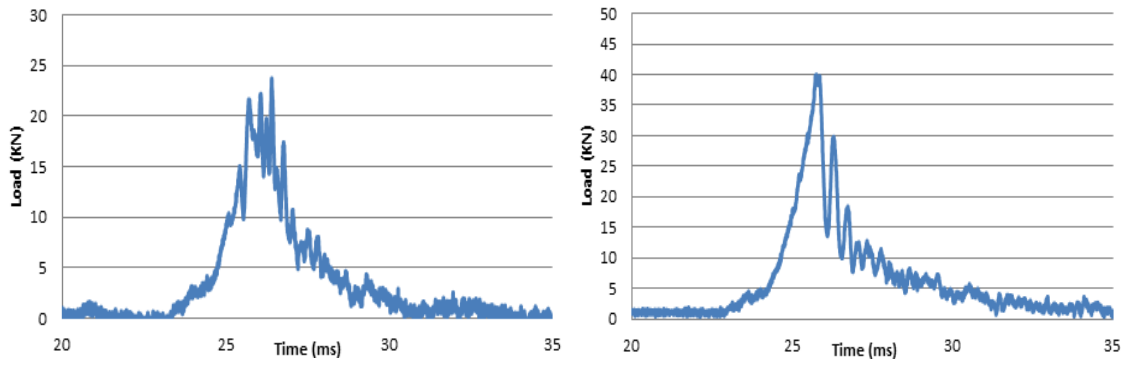
120 With the measured support load and beam deflection, the load-deflection curve can be  
121 formed, and beam toughness can be obtained by calculating area below the load-deflection  
122 curve. By adjusting hammer release height and layers of fibreboard, various strain rates can  
123 be obtained and its effect on UHPFRC beam toughness could be evaluated.

## 124 2.3 Results from drop hammer tests

125 In the tests, UHPFRC beams with 2%, 6% and 6% hybrid fibre volumes are used to study the  
126 strain rate effect on UHPFRC toughness. As mentioned above, various hammer release  
127 heights and layers of fibreboard are used to get different strain rates.

### 128 2.3.1 Investigation of measured support loads from tests

129 As above description, the loads measured from load cells are employed to generate load-  
130 deflection curve, and it is verified from the previous studies that this measured load could  
131 match well with the loads from the hammer, although more 'noises' appear in measured  
132 load from load cells [Millard et al. 2010]. Figure 2 depicts two measured loads from load  
133 cells, which were obtained from UHPFRC beams with 2% and 6% fibre volumes, with impact  
134 load generated by releasing hammer at 2m, and 2 layers of 10mm thick fibreboards on the  
135 top of beam. It can be seen that in both cases, the measured support load contains many  
136 'noisy' spurs. Therefore, before using these measured loads for the analysis, these spurs  
137 should be removed from the load measurements.



138

139 Figure 2 Measured supports loads from beam with 2% fibre volume (left) and 6% fibre volume (right)

140 In this analysis, the high-pass Butterworth signal filter was designed and applied to remove

141 these noises, with cut-off frequency of 500Hz. The cut-off frequency is selected based on

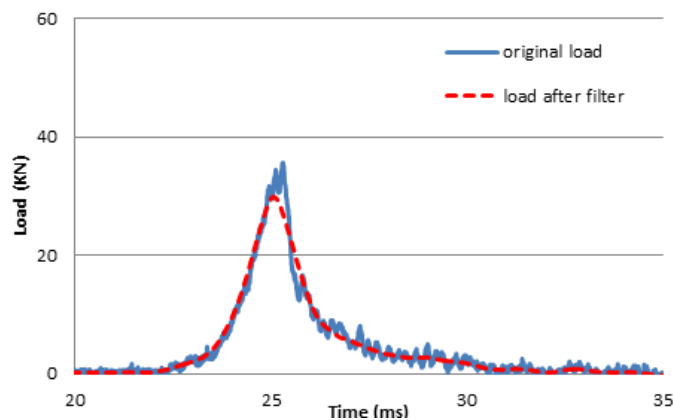
142 the natural frequencies of the UHPFRC beams (which is described in section 3.2), so that

143 information from the UHPFRC beams will not be removed with the filter. Figure 3 depicts

144 the original measured support load and processed support load after applying filter, it can

145 be seen that the spurs due to beam vibration can be removed effectively, and the support

146 load can better represent the impact load from drop hammer.



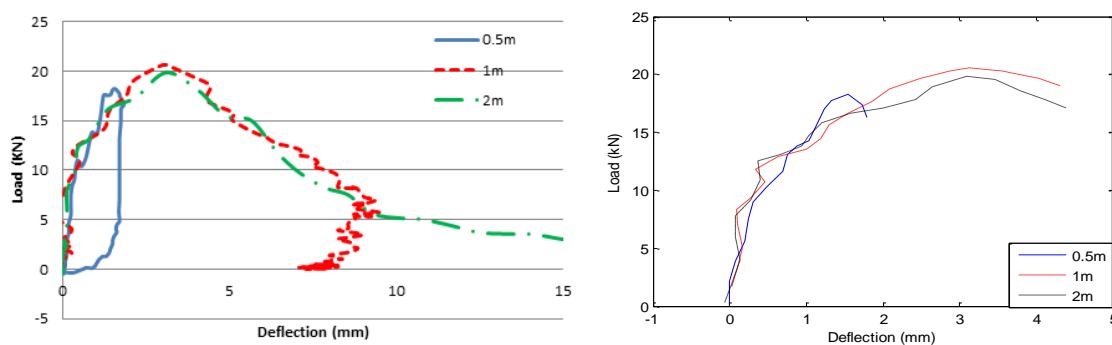
147

148 Figure 3 Comparison of support loads before and after applying filter

149 2.3.2 Strain rate effect on toughness of UHPFRC beam with 2% fibre volume



150 For UHPFRC beams with 2% fibre volume, drop hammer is released from 0.5m, 1m and 2m  
 151 to give different strain rates, and 2 layers of 10mm thick fibreboards are placed on the top  
 152 of beam to attenuate the applied load. For each case, support load after applying designed  
 153 filter and beam deflection are used to generate load-deflection curve, which is depicted in  
 154 Figure 4. It should be mentioned that for illustration purpose, only one load-deflection from  
 155 each case curve is shown in the figure, although several tests are repeated for each case.



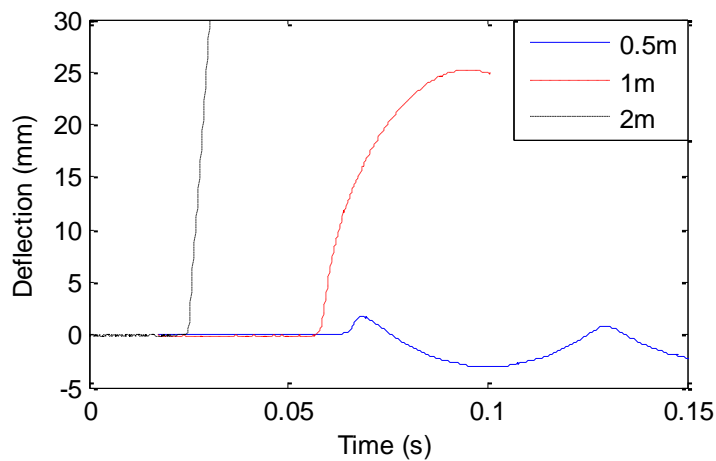
156

157 (a) Whole load-deflection curve (b) Load-deflection curve for toughness study

158 Figure 4 Load-deflection curves of UHPFRC beams with 2% fibre volume at various release heights

159 From Fig.4(a) it can be seen that hammer release height of 0.5m only give small deflection  
 160 of the UHPFRC specimen and strain hardening behaviour can not be observed. With  
 161 increased hammer release height, serious cracks in the specimen are found and strain  
 162 hardening is observed in the load-deflection curve. Moreover, the toughness of UHPFRC  
 163 specimen is studied and shown in Fig.4(b), the toughness does not show clearly toughness  
 164 change trend within the studied strain rate range. The possible reason is that as fibre is  
 165 randomly oriented and distributed in the specimen, which could affect flexural strength of  
 166 UHPFRC specimen (Stephanie et al. 2010), thus the increase trend in specimen toughness  
 167 may be masked by this random effect, this will be further investigated in the later part using  
 168 numerical study.

169 To further study the beam damages due to the impact hammer from various releasing  
170 heights, the beam mid-span deflections from different hammer releasing heights are  
171 depicted in Fig.5. It can be seen that 0.5m hammer releasing height does not cause  
172 significant damage to the specimen, as the specimen vibrates and return to the original  
173 position after the impact load, while permanent deformation can be found under impact  
174 load with 1m hammer release height, indicating the existence of severe damage to the  
175 specimen, with further increase of hammer releasing height to 2m, the specimen will be  
176 completely broken into 2 parts. It should be mentioned that in the UHPFRC specimen with 2%  
177 fibre volume, the impact hammer will cause the bending failure to the beam with the cracks  
178 at/near the beam mid-span.

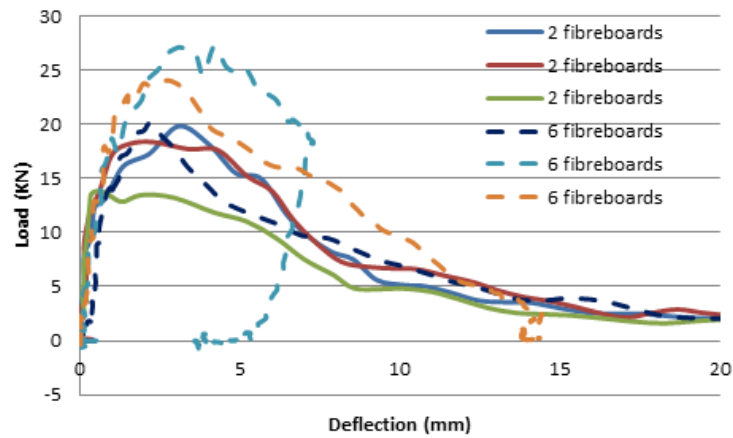


179

180 Figure 5 Mid-span deformation of UHPFRC beam with 2% fibre volume under various impact  
181 hammer releasing heights

182 Moreover, more layers of fibreboards are also used in the tests so that wider range of strain  
183 rates could be obtained. Two and six layers of fibreboards are employed for UHPFRC beams  
184 with 2% fibre volume, and hammer is released at 2m height, corresponding load-deflection

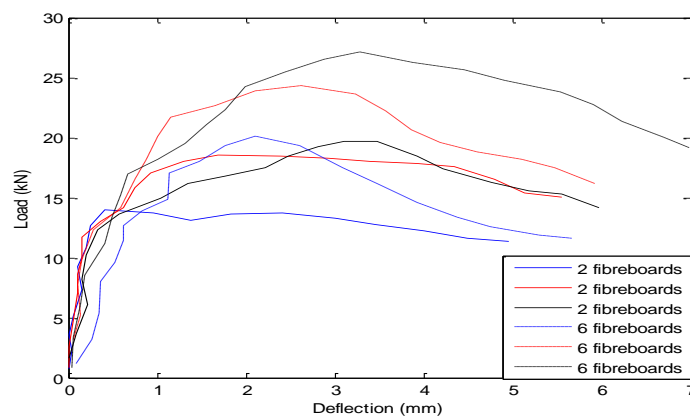
185 curves are depicted in Figure 6. For each case, three load-deflection curves are shown in  
186 Figure 5 to better illustrate the change of UHPFRC toughness.



187

188

(a) Whole load-deflection curve



189

190

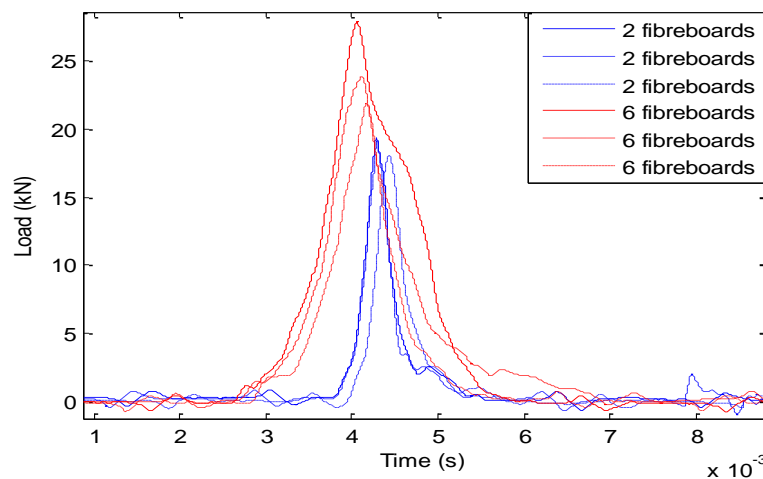
(b) Load-deflection curve for toughness study

191 Figure 6 Load-deflection curves of UHPFRC beams with 2% fibre volume at various layers of  
192 fibreboards

193 From Figure 6, with increased layers of fibreboards, which gives smaller strain rate values,  
194 the reduction of beam toughness can not be observed clearly, in some cases the UHPFRC  
195 beam with 6 fibreboards even give higher toughness, this can be found in Fig.6(b). Moreover,  
196 with 6 layers of fibreboards, most UHPFRC specimens still have complete fracture after the

197 impact load. It should be noted that the UHPFRC specimen with the same fibreboards give  
198 different load-deflection curve, this is caused by the effect of random fibre orientation and  
199 distribution, which may be the reason that the increase trend of specimen toughness with  
200 strain rate can not be observed.

201 Figure 7 depicts the time-history of impact load to the UHPFRC specimen with different  
202 number of fibreboards. It can be observed that with increase fibreboards (causing smaller  
203 strain rate), impact load with higher amplitude can be generated. Moreover, more  
204 fibreboards can give longer impact load duration and smaller loading rate to the UHPFRC  
205 specimen.

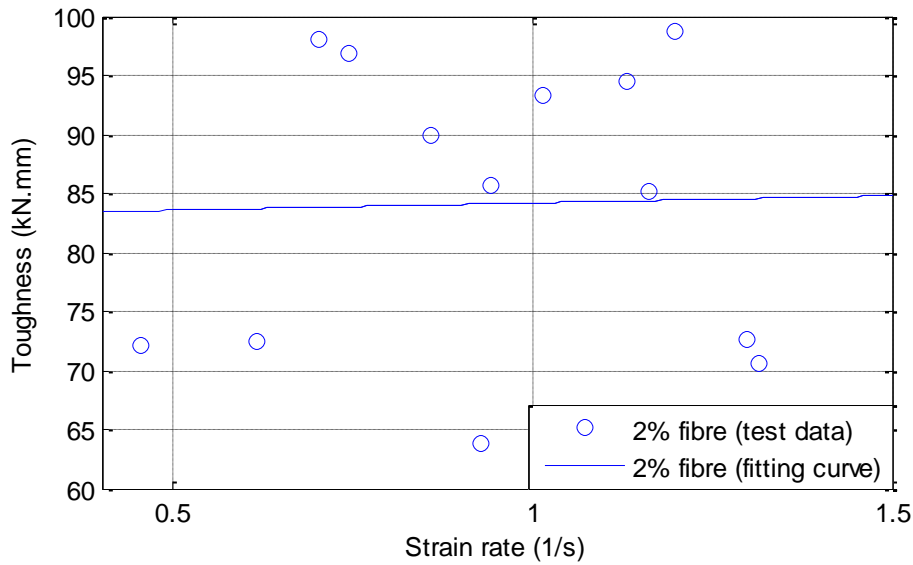


206

207 Figure 7 Time-history of impact load to 2% fibre volume UHPFRC specimen with different  
208 fibreboards

209 Moreover, in order to better illustrate the effect of strain rate on UHPFRC toughness, the  
210 strain rate and toughness (which is defined as the area below load-deflection curve) are  
211 calculated from each case, and toughness-strain rate relationship can be evaluated.

212 With this method, strain rate is calculated and its effect on toughness can be evaluated by  
213 studying the relationship between the UHPFRC beam toughness and strain rate, which is  
214 depicted in Figure 8, it should be noted that the exponential function is fitted to match the  
215 test data points.



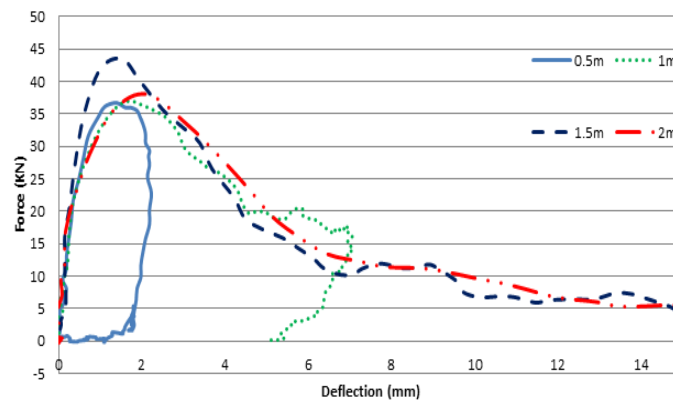
216  
217 Figure 8 Relationship of strain rate and absorbed energy of UHPFRC beams with 2% fibre volume

218 It can be seen from above figure that the strain rate increase trend cannot be found clearly  
219 with strain rate. Moreover, it should be noted that the curve starts with the strain rate of  
220  $0.4s^{-1}$ , the reason is that below this value, the beam only experience small deflection, and  
221 strain hardening can not be observed, thus the toughness is not included in the analysis.

222 As increase of UHPFRC specimen toughness with strain rate can not be observed with beam  
223 having 2% fibre volume, the UHPFRC beam containing higher fibre volume will be employed  
224 to obtain the toughness change with strain rate.

### 225 2.3.3 Strain rate effect on UHPFRC beam with 6% fibre volume

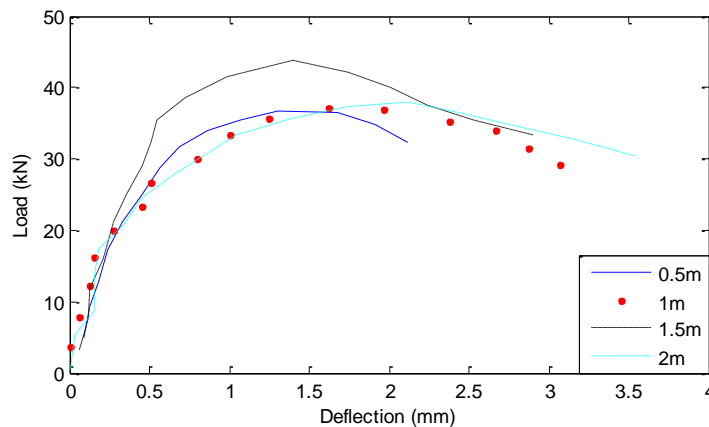
226 Similar to UHPFRC beam with 2% fibre volume, drop hammer is released at various heights  
 227 to get different strain rates, and load-deflection curves are obtained. 0.5m, 1m, 1.5m and  
 228 2m release heights are used and corresponding load-deflection curves are shown in Figure 9.  
 229 It should be mentioned that filter is applied to measured support loads to remove  
 230 component from beam vibration. Only one curve is depicted in each release height in order  
 231 to better express the change of beam toughness. 2 layers of 10mm thick fibreboards are  
 232 used in these cases to attenuate the hammer load.



233

234

(a) Whole load-deflection curve



235

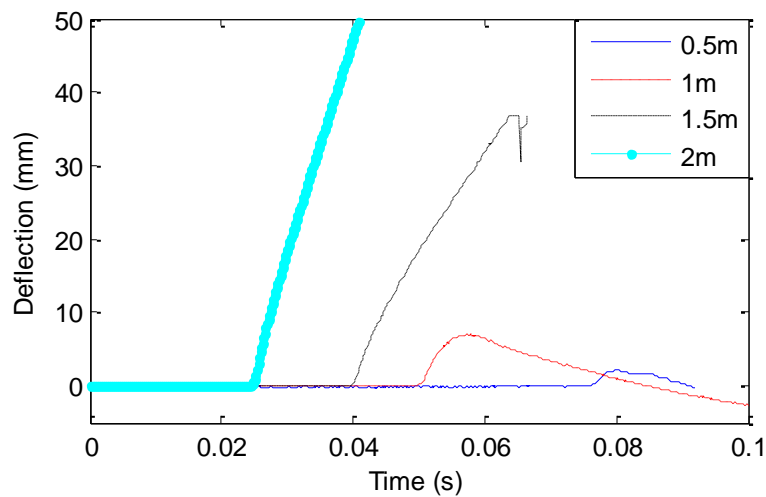
236

(b) Load-deflection curve for toughness study

237 Figure 9 Load-deflection curves of UHPFRC beams with 6% fibre volume at various release heights

238 From above Figure, it can be observed that the beam toughness increased with hammer  
239 release height from 0.5m to 1.5m, and increase trend at 2m hammer release height can not  
240 be seen due to the random effect of fibre orientation and distribution, which is similar to  
241 that in specimen with 2% fibre volume.

242 Furthermore, the mid-span deformation of specimen under various hammer releasing  
243 heights are depicted in Figure 10, and the specimen after the impact hammer is shown in  
244 Figure 11 to study the damage of UHPFRC specimen with 6% fibre volume due to the impact  
245 hammer.



246

247 Figure 10 Mid-span deformation of UHPFRC beam with 6% fibre volume under various

248

impact hammer releasing heights



249

250

Figure 11 UHPFRC specimen with 6% fibre volume after the impact test

251

It can be seen from Figure 10 that compared to the mid-span deformation of UHPFRC

252

specimen with 2% fibre volume (shown in Figure 5), UHPFRC specimen with 6% fibre volume

253

does not show severe damage under 1m high impact hammer, since permanent

254

deformation is not observed in this case, this indicate the effect of fibre volume in improve

255

the UHPFRC resistance to the impact load. With further increase hammer release height,

256

permanent deformation and severe damage can be found in UHPFRC specimen with impact

257

load of 1.5m release height, and under 2m high impact hammer, the UHPFRC specimen is

258

broken into 2 parts completely. Similar to UHPFRC specimen with 2% fibre volume, UHPFRC

259

specimen with 6% fibre volume shows the bending failure mode under the impact loading,

260

and the crack is observed at/near the mid-span of specimen, which is shown in Figure 11.

261

Moreover, the effect of fibreboard number on load-deflection curve is also investigated.

262

Two and five layers of fibreboards are used in the tests with 2m release height of drop

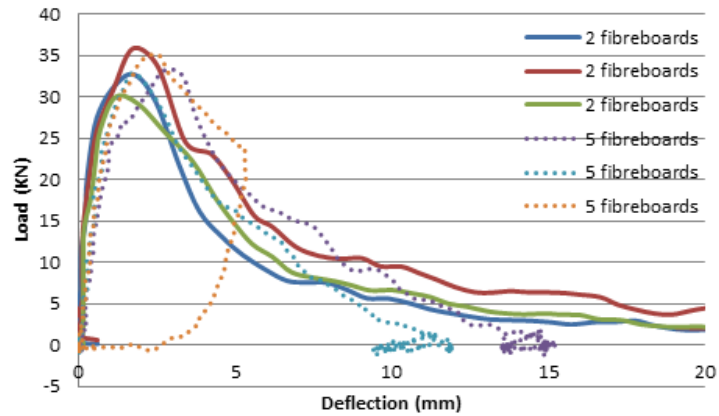
263

hammer to get various strain rate values. Figure 12 shows the load-deflection curves for two

264

and five layers of fibreboards cases.

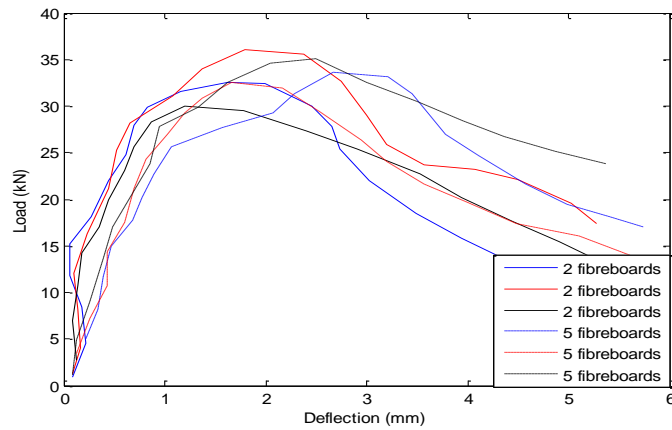




265

266

(a) Whole load-deflection curve



267

268

(b) Load-deflection curve for toughness study

269

Figure 12 Load-deflection curves of UHPFRC beams with 6% fibre volume at various layers of

270

fibreboards

271

It can be seen from above figure that with this method, the clearly increase trend of

272

specimen toughness with strain rate cannot be observed. It should be noted that the results

273

in UHPFRC specimen with 2% fibre volume (increased specimen toughness with reduced

274

strain rate) are not found in specimen with higher fibre volume.

275

Figure 13 shows the time-history of impact load to the 6% fibre volume UHPFRC specimen

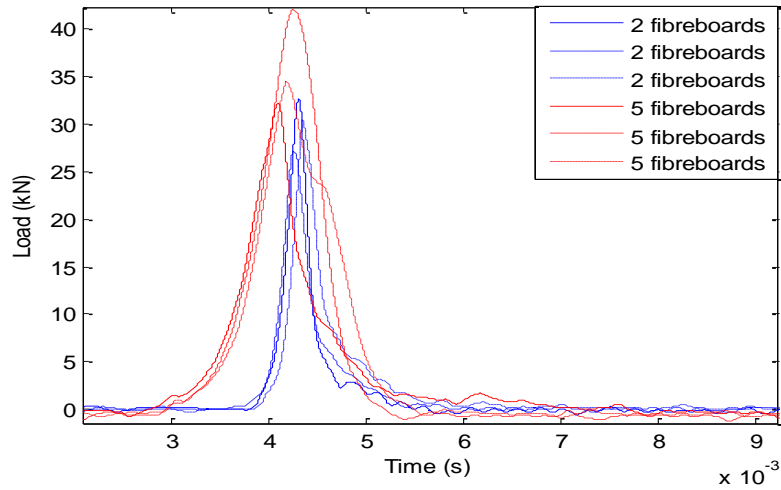
276

with different number of fibreboards. Similar to UHPFRC specimen with 2% fibre volume,

277

using more fibreboards can clearly increase the impact load duration, which can effectively

278 provide the lower impact loading rate. This is consistent to the results from UHPFRC  
279 specimen with 2% fibre volume.

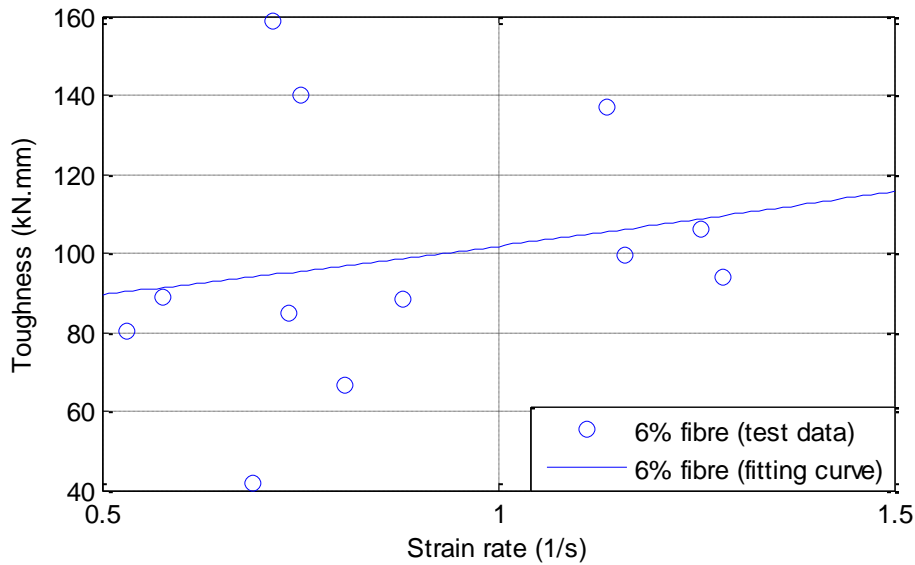


280

281 Figure 13 Time-history of impact load to 6% fibre volume UHPFRC specimen with different  
282 fibreboards

283 Furthermore, strain rate value is calculated in each test with bending beam theory and its  
284 effect on UHPFRC beam toughness is evaluated and depicted in Figure 14, and a curve is  
285 fitted to match the data points.

286



287

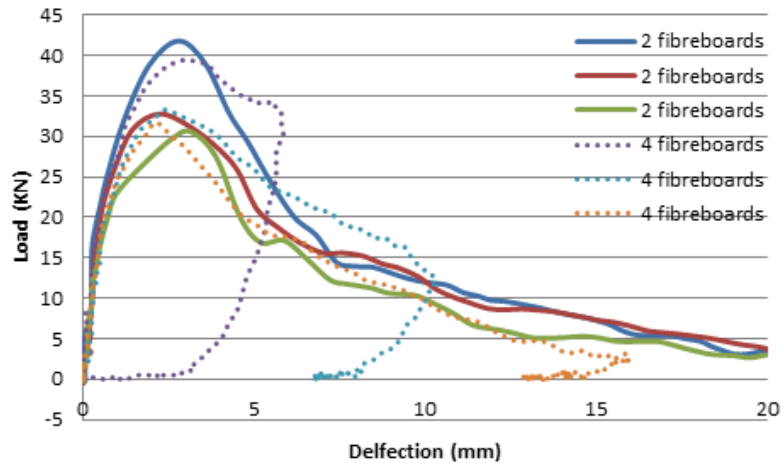
288 Figure 14 Relationship of strain rate and absorbed energy of UHPFRC beams with 6% fibre volume

289 From above figure, it can be observed that in the investigated range of strain rate, beam  
 290 toughness will increase with strain rate, but this trend is not clearly. It should be mentioned  
 291 that with increase of fibre volume, the beam resistance to impact loading will be increased  
 292 accordingly, this can be found with the starting strain rate in Fig.9, which is about  $0.6s^{-1}$ , as  
 293 below this value the beam experiences small deflection and can not express strain  
 294 hardening behaviour. Therefore, the increase of fibre volume can improve UHPFRC  
 295 performance and reduce the random effect due to fibre orientation and distribution.

296 2.3.4 Strain rate effect on UHPFRC beam with 6% hybrid fibre volume

297 In order to study the effect of fibre combination on UHPFRC behaviour, UHPFRC beams with  
 298 6% hybrid fibre volume are tested, and results are compared to those from beams with 6%  
 299 fibre volume. In the tests, two and four layers of fibreboards are employed to get different  
 300 strain rate values, and load-deflection curves from those tests are obtained and depicted in

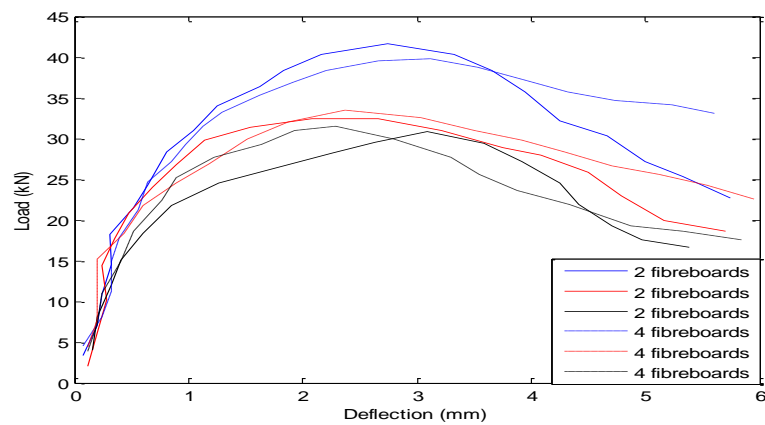
301 Figure 15. It should be mentioned that the release height of drop hammer is fixed to 2m for  
 302 UHPFRC beam with 6% hybrid fibre volume.



303

(a) Whole load-deflection curve

304



305

(b) Load-deflection curve for toughness study

306

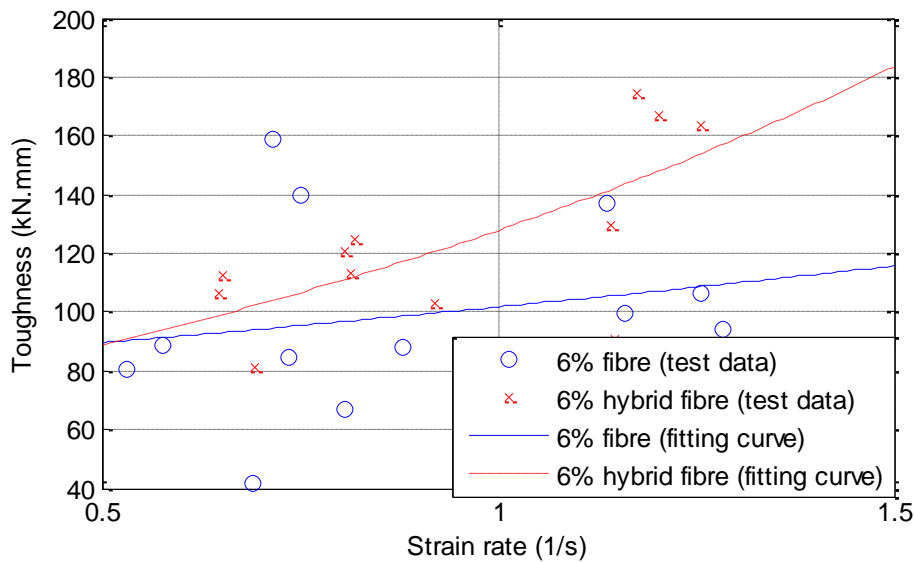
307 Figure 15 Load-deflection curves of UHPFRC beams with 6% hybrid fibre volume at various layers of  
 308 fibreboards

309 From above results, the increase of strain rate using reduced number of fibreboards can not  
 310 give higher specimen toughness, which is similar to results in UHPFRC specimen with 6%  
 311 fibre volume. Moreover, similar to UHPFRC beams with 6% fibre volume, all the tested

312 beams with 4 layers of fibreboards can survive the impact loading without complete  
313 fracture.

314 In order to better illustrate the effects of fibre combination, the beam toughness-strain rate  
315 curves for UHPFRC beams with 6% fibre and 6% hybrid fibre volumes are compared and  
316 depicted in Figure 16. It can be seen that the use of fibre combination in this study can  
317 increase the UHPFRC specimen toughness, but this effect is not clearly.

318



319

320 Figure 16 Comparison of UHPFRC absorbed energy-strain rates curves from UHPFRC beams with 6%  
321 fibre volume and 6% hybrid fibre volume

322 From above results, it can be concluded that the increase of fibre volume can improve the  
323 UHPFRC specimen resistance effectively, UHPFRC specimen with 2% fibre volume  
324 experiences complete fracture at strain rate of  $0.4s^{-1}$ , while UHPFRC specimen with 6%  
325 fibre volume is broken into two parts at  $0.6s^{-1}$  strain rate. Moreover, with UHPFRC  
326 specimen containing higher fibre volume, the increase of specimen toughness with strain

327 rate can be observed, this indicate effect due to fibre random orientation and distribution  
328 can be reduced with increase of fibre volume. However, the use of fibre combination  
329 (different fibre lengths in this study) can increase the UHPFRC toughness, especially at high  
330 strain rate range.

### 331 3. Numerical study of UHPFRC beam toughness with strain rate

332 In the above section, experimental study is used to investigate the flexural toughness of  
333 UHPFRC beam by measuring support load and beam deflection. In the tests, several  
334 methods, including using different fibreboard layers, releasing hammer from various heights,  
335 are employed to get strain rates from  $0.2s^{-1}$  to  $1.5s^{-1}$  .

336 However, in the tests, the fibre orientation and distribution was not measured in UHPFRC  
337 beams, which may prevent the clearly relationship between UHPFRC toughness and strain  
338 rate, as the random fibre orientation and distribution may cause variation in the UHPFRC  
339 behaviour [Stephanie, et al. 2010, Mao, et al. 2015]. Therefore, in order to further  
340 investigate the evolution of beam toughness with strain rate, numerical method is  
341 employed herein to remove the influence due to random fibre orientation and distribution.

#### 342 3.1 Development of numerical model

343 In this study, the concrete damage model, also called K&C model, in LS-DYNA is used to  
344 simulate behaviour of UHPFRC beam. In K&C model, three independent strength surfaces,  
345 including initial yield, maximum failure, and residual surfaces, are defined, strain hardening  
346 and softening behaviours can also be expressed with strength surfaces interpolated between three  
347 defined strength surfaces, and strain rate effect can be expressed by defining strength  
348 enhancements in compression and tension separately (Malvar et al. 1997, 2000, Tu and Lu, 2009).

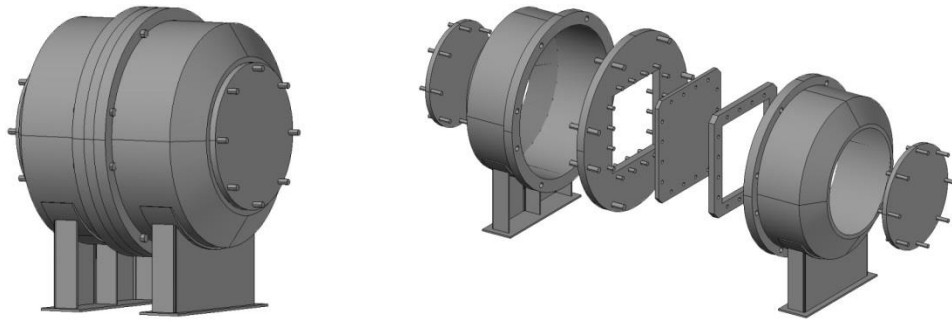
349 The capability of K&C model in simulating concrete materials under various loading  
350 conditions has already been investigated by previous studies (Tanapornraweekit et al. 2007,  
351 Odeh, 2008). Results demonstrated that the behaviour of normal strength concrete can be  
352 modelled with good quality with K&C model.

353 An important reason of using K&C model is that it contains an automatic model generation  
354 method. With this method, only concrete compressive strength is required, and all other  
355 concrete properties can be calculated automatically. This makes K&C model suitable in this  
356 study, as only limited UHPFRC properties are measured from tests (Magallanes et al. 2010).

357 However, it should be mentioned that the automatic model parameter generation method  
358 is developed based on test data from normal strength concrete (with compressive strength  
359 of about 35MPa), when it is applied to UHPFRC, even with input UHPFRC compressive  
360 strength (about 170MPa), the behaviour of developed model may not express actual  
361 UHPFRC performance, especially improved strain hardening and softening behaviours of  
362 UHPFRC. Therefore, after generating model parameters automatically, further modifications  
363 should be performed to the generated parameters, especially those controlling strain  
364 hardening and softening behaviours, to better express UHPFRC properties.

365 In this study, the static test is performed to obtain the material properties for the numerical  
366 modelling, from the test pressure-deflection curve of UHPFRC specimen can be obtained.

367 In the test, the UHPFRC slab with dimension of 660 x 660 x 25 mm was tested by uniformly  
368 distributed loading in a pulse pressure loading rig, developed by University of Liverpool (Schleyer, et  
369 al. 2012), which is depicted in Figure 17.



370

371

(a) Assembled view

(b) Expanded view

372

Figure 17 Pulse pressure loading rig (PPLR) used in static mode

373

The UHPFRC specimen was mounted in the central section of the loading rig with a rubber

374

strip used to provide an air tight around the edge of 500mm square loaded area. The central

375

deflection of UHPFRC specimen was measured with a linear variable differential transformer

376

(LVDT), and the pressure applied to UHPFRC specimen was measured using pressure gauges.

377

In the test, one side of the rig was pressurised with air in stages and the specimen deflection

378

was recorded at each loading step. Figure 18 shows the collected pressure-deflection curves

379

from UHPFRC specimen with different fibre volumes. It can be seen that the failure of

380

specimen cannot be controlled due to the means of loading, thus when the specimen

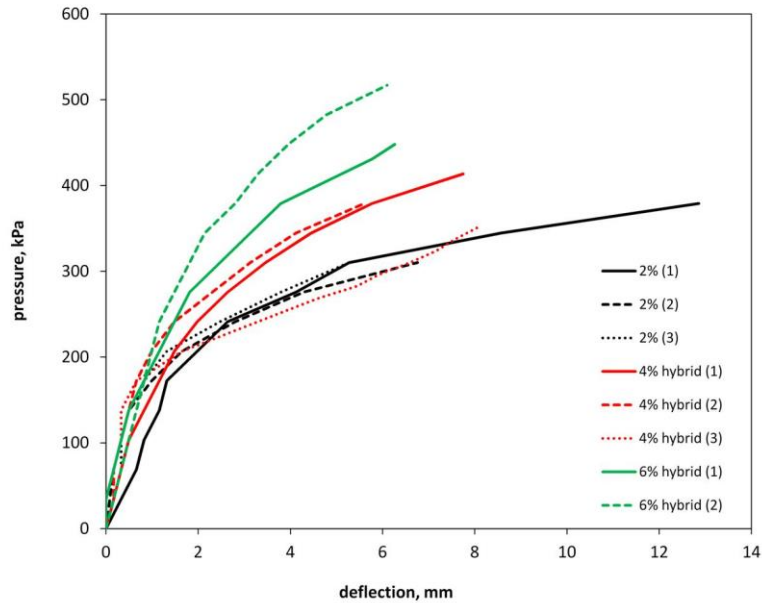
381

ruptured abruptly when it was tested to failure, it was not possible to obtain the data in the

382

strain-softening region for the complete pressure-deflection curve.

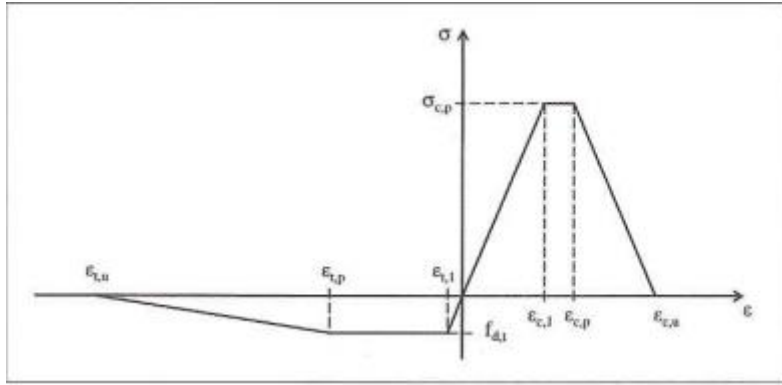




383

384 Figure 18 Pressure-deflection relationships for UHPFRC specimen obtained under static uniformly  
 385 distributed loading

386 Due to the fact that complete information about UHPFRC material properties cannot be  
 387 collected from the tests, the design stress-strain curve from UHPFRC with 2% fibre volume is  
 388 employed for the modification of generated model parameters, which is depicted in Figure  
 389 19, and Table 2 lists some key values of the design curve. Using this design curve, the  
 390 numerical model of UHPFRC beam with 2% fibre volume can be developed directly, model  
 391 parameters controlling strain hardening and softening are modified to let the modelled  
 392 stress-strain curve matches the design stress-strain relationship, while for UHPFRC beam  
 393 with 6% and 6% hybrid fibre volumes, as increased fibre volumes may not only change  
 394 compressive strength of UHPFRC, but also its stress-strain shape (Barnett et al. 2010), thus  
 395 the increased compressive strength and updated design stress-strain curve should be  
 396 applied to modify model parameters of UHPFRC beam model with 6% fibre volumes.



397

398

Figure 19 Design stress strain curve from UHPFRC with 2% fibre volume

399

Table 2 Material Properties of UHPFRC slab

Tension		Compression	
Tensile strength ( $f_{d,t}$ ) with 2% fibre volume	10MPa	Compressive strength ( $\sigma_{c,p}$ ) with 2% fibre volume	170MPa
Tensile strength ( $f_{d,t}$ ) with 6% fibre volume	15MPa	Compressive strength ( $\sigma_{c,p}$ ) with 6% fibre volume	200MPa
Max linear strain ( $\epsilon_{t,l}$ )	0.00011	Max linear strain ( $\epsilon_{c,l}$ )	0.0031
Limiting tensile strain ( $\epsilon_{t,p}$ )	0.004	Limiting compressive strain ( $\epsilon_{c,p}$ )	0.004
Max tensile strain ( $\epsilon_{t,u}$ )	0.01	Max compressive strain ( $\epsilon_{c,u}$ )	0.007

400

401 According to previous study (Mao, et al. 2014), the variation of DIF value with strain rate  
 402 under compression and tension can be expressed as:

$$403 \quad \text{Compression } DIF = \begin{cases} \left(\frac{\dot{\varepsilon}}{\dot{\varepsilon}_s}\right)^{1.026\alpha} & \dot{\varepsilon} \ll \dot{\varepsilon}_1 \\ A_1 \ln(\dot{\varepsilon}) - A_2 & \dot{\varepsilon} > \dot{\varepsilon}_1 \end{cases} \quad (1)$$

404 where  $\dot{\varepsilon}$  is strain rate,  $\dot{\varepsilon}_s = 3 \times 10^{-5} s^{-1}$  is the quasi-static strain rate,  $\alpha = 1/(20 + f_{cs}/2)$ ,  
 405  $f_{cs}$  is the static compressive strength,  $\dot{\varepsilon}_1 = 0.0022f_{cs}^2 - 0.1989f_{cs} + 46.437$  ( $\dot{\varepsilon}_1$  is  $79s^{-1}$  in  
 406 this case),  $A_1 = -0.0044f_{cs} + 0.9866$ ,  $A_2 = -0.0128f_{cs} + 2.1396$ .

$$407 \quad \text{Tension } DIF = \begin{cases} \left(\frac{\dot{\varepsilon}}{\dot{\varepsilon}_s}\right)^\delta & \dot{\varepsilon} \ll 30s^{-1} \\ \beta \left(\frac{\dot{\varepsilon}}{\dot{\varepsilon}_s}\right)^{1/3} & \dot{\varepsilon} > 30s^{-1} \end{cases} \quad (2)$$

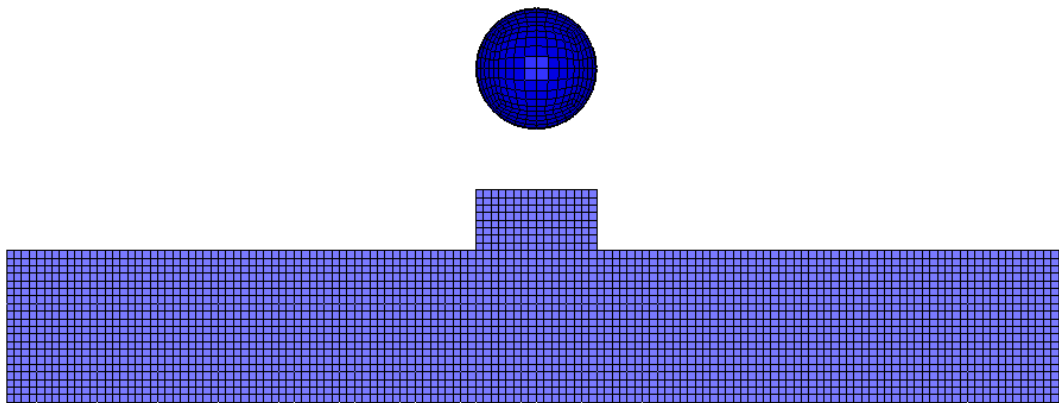
408 where  $\dot{\varepsilon}_s = 10^{-6} s^{-1}$ ,  $\log \beta = 7.11\delta - 2.33$ ,  $\delta = 1/(10 + 6f_{cs}/f_{co})$ ,  $f_{cs}$  is the static  
 409 concrete compressive strength,  $f_{co} = 10MPa$ .

410 Several simplifications were made in the study to reduce the complexity of UHPFRC model  
 411 without affecting final results (Mao, et al. 2014). Steel fibres are not modelled explicitly, and  
 412 its effect is achieved by matching the modelled stress-strain curve from homogeneous  
 413 model to design stress-strain relationship of UHPFRC. Moreover, in the model, the supports  
 414 are not simulated, and the UHPFRC beam is simply supported by constraining vertical  
 415 displacement of supported area. It should be mentioned that in the numerical study, only  
 416 UHPFRC beams with 2% and 6% fibre volumes were investigated due to limited information  
 417 from UHPFRC specimen with 6% hybrid fibre volume.

418 It should be mentioned that the performance of K&C model in predicting UHPFRC behaviour  
 419 under blast loading have been studied in some previous researches (Mao, et al. 2014, 2015),

420 where both the deflection and failure mode of UHPFRC specimen can be predicted with  
421 good quality.

422 Figure 20 depicts the developed UHPFRC beam model, the drop hammer is modelled as  
423 sphere shape using \*MAT\_ELASTIC model, which can give same contact area as in the tests,  
424 and fibreboard is modelled with \*MAT\_PLASTIC\_KINEMATIC model. Moreover, element size  
425 of beam model is selected as 2.5mm×2.5mm×2.5m after mesh convergence study.



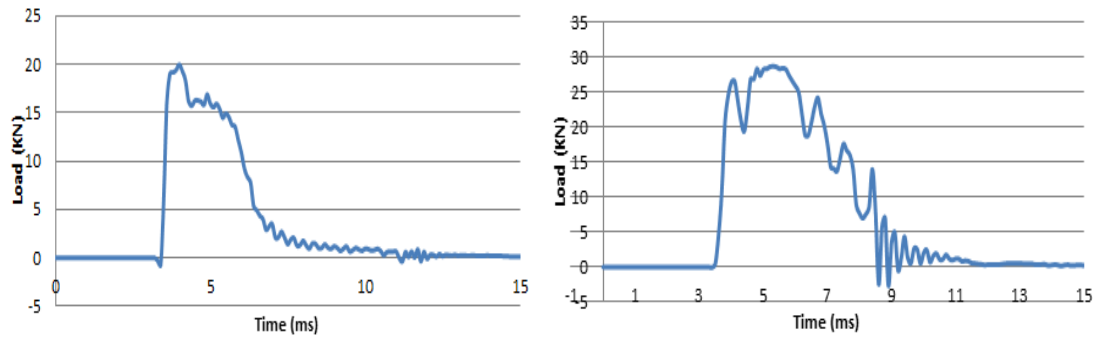
426

427 Figure 20 Developed UHPFRC beam model

### 428 3.2 Numerical investigation of support load

429 From section 2, it can be seen that the measured support load contain noisy spurs, and  
430 high-pass filter is applied to remove these spurs. In this section, the developed model will be  
431 employed to study the information in the support load, and extract natural frequencies of  
432 UHPFRC to evaluate its condition after the impact load.

433 Figure 21 depicts modelled support loads from beams with 2% and 6% fibre volumes (with  
434 1m hammer releasing height). From the figure, spurs still appear in the support load.  
435 Moreover, more spurs can be found in the support load from beam with 6% fibre volume.



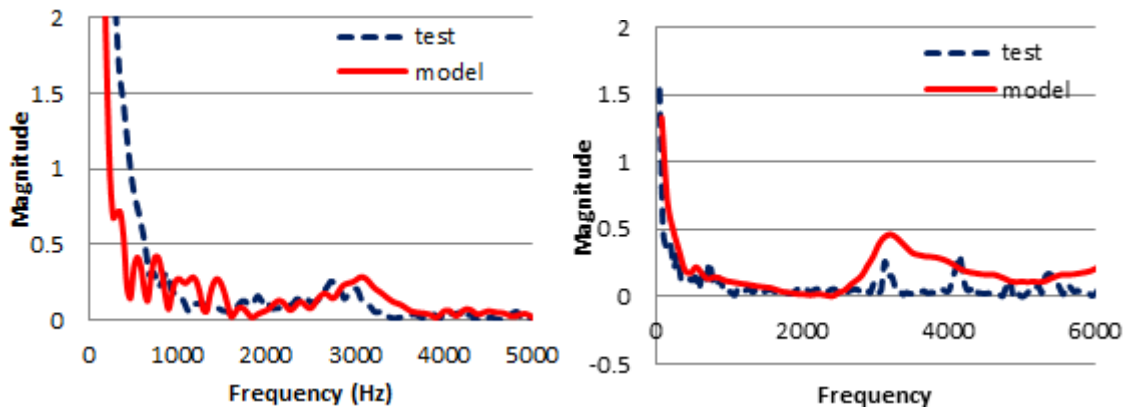
436

437 Figure 21 Support loads from developed beams with 2% fibre volume (left) and 6% fibre volume  
 438 (right)

439 It can be seen from Figure 21 that before the impact load, a negative reaction force is  
 440 appeared in the UHPFRC model with 2% fibre volume before the positive reaction force, this  
 441 is due to the inertia effect which can give a value in opposite phase with impact load  
 442 [Cotsovos, 2010, Kishi and Mikami, 2012]. However, it should be noted that this negative  
 443 reaction force cannot be observed in UHPFRC model with 6% fibre volume, the reason is  
 444 that the increase of fibre volume can improve the UHPFRC resistance to the impact load  
 445 effectively, thus less inertia effect can be excited with the same impact load. Moreover, it  
 446 can be seen that due to the inertia force in the UHPFRC model, the impact load will show  
 447 several fluctuations after the peak load value. This can be used to confirm that the inertia  
 448 effect is included in the developed UHPFRC model, and the model can be used to study the  
 449 UHPFRC dynamic behaviour under impact loading condition effectively.

450 With the developed model, the first few natural frequencies from UHPFRC beam with 2%  
 451 fibre volume are extracted, these frequencies are then compared to those from tested data,  
 452 Figure 22 depicts the comparison results of power spectrum from whole support load and  
 453 free vibration part after cutting support load. Similar frequency peak around 3000Hz can be

454 found in both curves, which confirms that the developed model can provide reliable the  
455 behaviour of UHPFRC beam under impact loading.



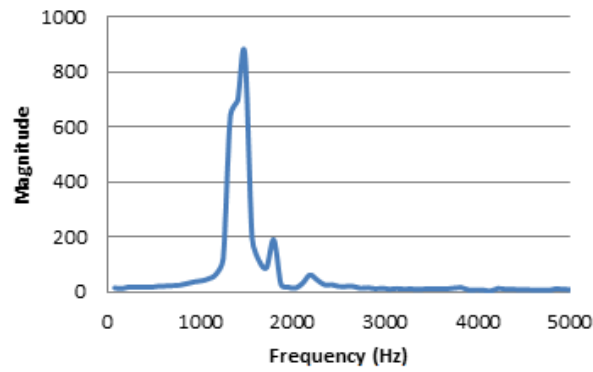
456

457 (a) Power spectrums of whole support load (b) Power spectrums of cutted support load

458

Figure 22 Comparison of power spectrums from tested and modelled support loads

459 However, by comparing it with the natural frequencies of intact UHPFRC beam, which were  
460 obtained from developed model with modal analysis and listed in Table 3 (Table 3 also  
461 includes frequencies from power spectrum of tested support load of UHPFRC beam with 6%  
462 fibre volume), the 1<sup>st</sup> natural frequency of the UHPFRC beam cannot be found in Figure 22,  
463 the reason that in the above case, the beam is damaged completely after the impact loading.  
464 For further confirm the performance of developed model, the frequencies in the support  
465 load of with 0.5m impact hammer release height are extracted, where the UHPFRC beam  
466 with 6% fibre volume only experiences minor damage, the results are depicted in Figure 23.  
467 It can be seen that the 1<sup>st</sup> natural frequency at about 1300Hz can be observed clearly, which  
468 further validates the performance of the developed model.



469

470

Figure 23 Power spectrum of support load from model at 0.5m high drop hammer

471

Table 3 Natural frequencies of UHPFRC beam

Mode	Modelled UHPFRC beam with 2% fibre volume	Modelled UHPFRC beam with 6% fibre volume	Tested UHPFRC beam with 6% fibre volume
1 <sup>st</sup> bending mode	1237.9Hz	1284.9Hz	732Hz
1 <sup>st</sup> torsion mode	3499.4Hz	3643Hz	3125Hz
2 <sup>nd</sup> bending mode	4239.1Hz	4413.6Hz	4150Hz
2 <sup>nd</sup> torsion mode	7019.2Hz	7309.5Hz	5422Hz

472

473

Moreover, from results in Table 3, it can be seen that from the tests, after the impact

474

loading, natural frequencies from the first few modes can still be extracted from UHPFRC

475

beam with 6% fibre volume, but compared to the numerical natural frequencies, significant

476

reduction can be observed. As the 1st natural frequency of beam can be calculated with the

477

following equation, the beam condition after impact load can be evaluated:

478

$$\omega_n = A\sqrt{EI/\mu L^4} \quad (3)$$

479 where A is the constant value and will be changed for different boundary conditions, E is  
480 Young's modulus, I is area moment of inertia, L is beam length, and  $\mu$  is mass per unit beam  
481 length.

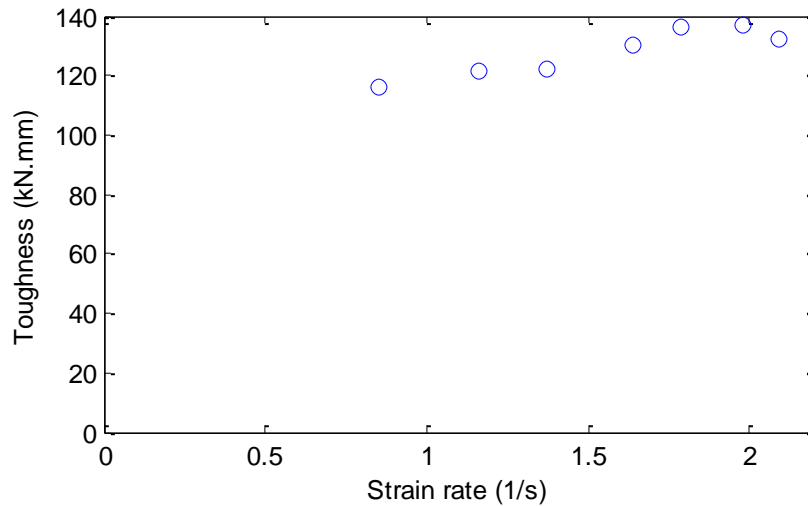
482 By comparing natural frequencies of beam before and after impact load, it can be estimated  
483 that after the impact load, rigidity (EI) of damaged beam is only 32% of its original value, this  
484 can be used to evaluate the damage level and the remaining strength of the beam.

### 485 3.3 Numerical results of UHPFRC beams with 2% fibre volume

486 As described in section 3.1, UHPFRC beam model with 2% fibre volume is developed and its  
487 stress-strain relationship is modified to match the design curve. It should be mentioned that  
488 the same procedure is used to obtain the relationship between strain rate and toughness,  
489 i.e. impact hammer is released to the UHPFRC beam, and load-deflection curve can be  
490 obtained. From the results, the toughness can be calculated using the area below the load-  
491 deflection curve, while strain rate is obtained by reading strain rate time-history from  
492 middle element on the beam bottom surface in LS-DYNA results.

493 In the model, various strain rates are obtained by releasing hammer from different heights,  
494 which is achieved by defining velocity of the drop hammer based on corresponding  
495 releasing height. From the results, the strain rate-toughness curve can be generated, which  
496 is depicted in Figure 24.





497

498 Figure 24 Relationship of strain rate and absorbed energy of UHPFRC beams with 2% fibre volume

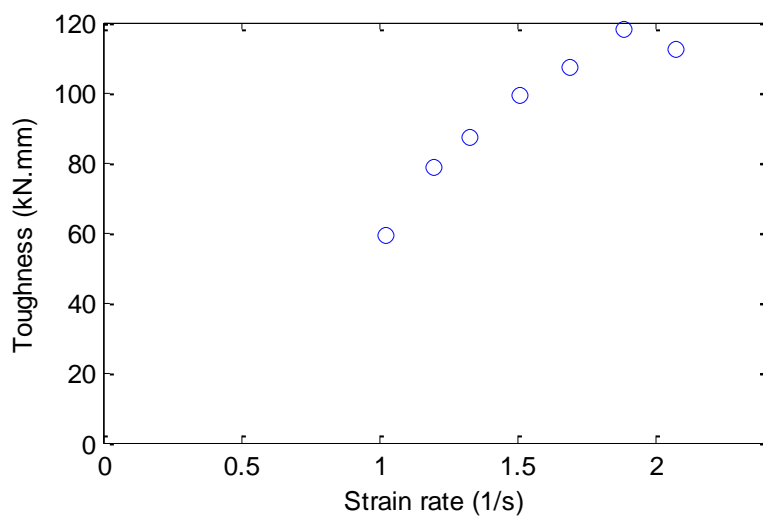
499 from model

500 From above results, it can be observed that the toughness of UHPFRC specimen will increase  
 501 with strain rate. It should be noted that this increase trend is not clearly, thus it can be  
 502 masked by the random effect of fibre orientation and distribution in the test results shown  
 503 in section 2.

### 504 3.4 Numerical results of UHPFRC beams with 6% fibre volume

505 As mentioned in section 3.1, when modelling UHPFRC beam with 2% fibre volume, the  
 506 design stress-strain curve (shown in Figure 19) can be used directly, as the design curve is  
 507 from UHPFRC specimen with 2% fibre volume, while for UHPFRC beam with 6% fibre volume,  
 508 the stress-strain curve should be changed due to increase of fibre volume, not only for  
 509 concrete strength, but also for the shape of curve. In this study, without stress-strain curve  
 510 from UHPFRC specimen with 6% fibre volume, the concrete compressive and tensile  
 511 strengths are increased for UHPFRC beam with 6% fibre volume (listed in Table 2), and

512 model parameters controlling strain hardening and softening behaviours are modified to  
513 match the tested force-deflection curve from UHPFRC beam with 6% fibre volume.  
514 Similar to UHPFRC beam cases with 2% fibre volume, beam toughness vs. strain rate  
515 relationship is obtained using developed UHPFRC beam model with 6% fibre volume using  
516 the same procedure. Figure 25 shows the relationship of beam toughness and strain rate  
517 from beam with 6% fibre volume.



518  
519 Figure 25 Relationship of strain rate and absorbed energy of UHPFRC beams with 6% fibre volume  
520 from model

521 From above figure clearly increase trend of toughness is observed, indicating increased fibre  
522 volume in UHPFRC specimen can give more significant strain rate effect. Moreover, UHPFRC  
523 specimen with 6% fibre volume shows improved resistance to impact load, this can be found  
524 that the starting strain rate is higher than  $1s^{-1}$  in Fig.20, where the specimen has complete  
525 fracture, this value is larger than the strain rate leading to collapse of UHPFRC specimen  
526 with 2% fibre volume

527 Furthermore, the root mean square error (RMSE) is used to evaluate the toughness from  
 528 the developed UHPFRC model, which can be calculated as follows, and results are listed in  
 529 Table 4.

$$530 \quad RMSE = \sqrt{\frac{\sum_{i=1}^n (\hat{y}_i - y_i)^2}{n}} \quad (1)$$

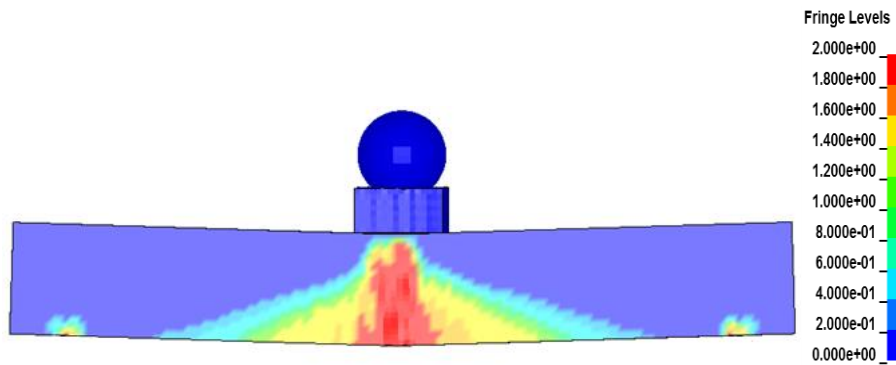
531 Where  $n$  is the number of measurements (number of toughness values herein),  $y_i$  and  $\hat{y}_i$   
 532 are the toughness values from the measurement and developed model at the same strain  
 533 rate, respectively.

534 Table 4 Root mean square error between tested and simulated toughness-strain rate relationships

Fibre volume in UHPFRC specimen	Number of toughness values	RMSE
2%	13	20.07
6%	12	13.39

535  
 536 It can be seen from Table 4 that high RMSE values are observed, the reason is that in the  
 537 test, the toughness value may show great variation even at the same strain rate, which is  
 538 caused by the effect of random fibre orientation and distribution. With further increase of  
 539 fibre volume in UHPFRC specimen, this random effect can be reduced effectively, and  
 540 smaller RMSE value can be obtained for UHPFRC with 6% fibre volume. This further confirms  
 541 the necessity of using numerical model for the better understanding of UHPFRC behaviour  
 542 under high strain rate loads.

543 Moreover, the crack pattern of UHPFRC beam model with 6% fibre volume is shown in  
544 Figure 26, where bending failure mode can be observed, and severe damage (cracks) are  
545 located at mid-span of the UHPFRC beam, which is consistent to the results observed from  
546 the tests (shown in Figure 11). This indicates the effectiveness of using UHPFRC model for  
547 predicting UHPFRC behaviour and crack pattern under high strain rate loads.



548

549 Figure 26 Damage of UHPFRC model with 6% fibre volume under impact loading

#### 550 4. Conclusions

551 In this paper, and the evolution of UHPFRC beam toughness with strain rate is investigated  
552 using both experimental and numerical studies. UHPFRC beams with various fibre volumes  
553 are employed for the analysis. In the experimental tests, various hammer release heights  
554 and fibreboard layers are employed to get a set of strain rates.

555 With test data, UHPFRC beam toughness and corresponding strain rate can be obtained.

556 From the results, the increase of UHPFRC (with 2% fibre volume) toughness with strain rate  
557 cannot be observed clearly.

558 With increased fibre volume in UHPFRC specimen, the toughness increase trend with strain  
559 rate can be observed, and the blast resistance of UHPFRC specimen is also increased.

560 Moreover, the effect of fibre with different lengths is studied, results demonstrate that the  
561 UHPFRC beam with fibre combination can only give slight higher toughness, especially at  
562 high strain rate range.

563 Considering the influence of random fibre orientation and distribution is not considered in  
564 the tests, numerical analysis is performed in LS-DYNA to further study the beam toughness  
565 with increased strain rate. A UHPFRC beam model is developed and its performance under  
566 impact load is validated, in the model, the parameters controlling strain hardening and  
567 softening behaviours are modified to match stress-strain relationship from UHPFRC  
568 specimen. Results show increased UHPFRC toughness with strain rate from specimen with  
569 both 2% and 6% fibre volumes, while UHPFRC specimen with high fibre volume will give  
570 more clearly toughness increase trend, and strain rate effect and blast resistance are  
571 improved with increase of fibre volume in UHPFRC specimen.

## 572 Acknowledgements

573 The authors are grateful to the Faculty of Technology and School of Civil Engineering and  
574 Surveying at the University of Portsmouth for financial support. The test data described  
575 here was collected as part of an EPSRC-funded project at the University of Liverpool. The  
576 authors gratefully acknowledge the significant contributions to this work by Professor Steve  
577 Millard (formerly University of Liverpool), Bekaert, VSL Australia, CPNI and GL Industrial  
578 Services.

## 579 Reference

580 Barnett, S.J. Development of advanced concrete materials for anti-terrorism applications.  
581 The Structural Engineer, October 7, 2008, 28-29.

582 Barnett, S.J., Lataste, J.F., Parry, T., Millard, S.G., Soutsos, M.N. Assessment of fibre  
583 orientation in ultra high performance fibre reinforced concrete and its effect on flexural  
584 strength. *Materials and Structures*, 2010, 43(7): 1009-1023.

585 Bragov, A.M., Petrov, Y.V., Karihaloo, B.L., Konstantinov, A.Y., Lamzin, D.A., Lomunov, A.K.,  
586 Smirnov, I.V. Dynamic strengths and toughness of an ultra high performance fibre reinforced  
587 concrete. *Engineering Fracture Mechanics*, 2013, 110, 477-488.

588 Cotsovos, D.M. A simplified approach for assessing the load-carrying capacity of reinforced  
589 concrete beams under concentrated load applied at high rates. *International Journal of*  
590 *Impact Engineering*, 2010, 37(8), 907-917.

591 Habel, K., Viviani, M., Denarie, E., Bruhwiler, E. Development of the mechanical properties  
592 of an ultra-high performance fiber reinforced concrete (UHPFRC). *Cement and Concrete*  
593 *Research*, 2006, 36(7), 1362-1370.

594 Isaacs, J., Magallanes, J., Rebentrost, M., Wight, G. Exploratory dynamic material  
595 characterizing tests on ultra-high performance fiber reinforced concrete. 8th International  
596 Conference on Shock & Impact loads on structures, December 2-4, 2009, Adelaide, Australia.

597 Kang, S.T., Lee, Y., Park, Y.D., Kim, J.K. Tensile fracture properties of an ultra high  
598 performance fiber reinforced concrete (UHPFRC) with steel fiber. *Composite Structures*,  
599 2010, 92(1), 61-71.

600 Kim, D.J., Park, S.H., Ryu, G.S., Koh, K.T. Comparative flexural behaviour of hybrid ultra high  
601 performance fiber reinforced concrete with different macro fibers. *Construction and*  
602 *Building Materials*, 2011, 25(11), 4144-4155.

603 Kishi, N., Mikami, H. Empirical formulas for designing reinforced concrete beams under  
604 impact loading. *ACI Structural Journal*, 2012, 109(4), 509-520.

605 Magallanes, J.M., Wu, Y., Malvar, L.J., Crawford, J.E. Recent improvement to release III of  
606 the K&C concrete model, June 6-8, 2010, Dearborn, Michigan, USA.

607 Malvar, L.J., Crawford, J.E., Wesevich, J.W., Simons, D. A plasticity concrete material model  
608 for DYNA3D. *International Journal of Impact Engineering*, 1998, (9-10), 847-873.

609 Malvar, L.J., Crawford, J.E., Morrill, K.B. K&C concrete material model release III –  
610 automated generation of material model input. K&C Technical Report TR-99-24-B1,  
611 Glendale, CA, 2000.

612 Mao, L., Barnett, S.J., Begg, D., Schleyer, G.K., Wight, G. Numerical simulation of ultra high  
613 performance fibre reinforced concrete panel subjected to blast loading. *Journal of cement  
614 and concrete composites*, 2014, 64: 91-100.

615 Mao, L., Barnett, S.J., Tyas, A., Warren, J., Schleyer, G.K., Zaini, S.S. Response of small scale  
616 ultra high performance fibre reinforced concrete slabs to blast loading. *Construction and  
617 Building Materials*, 2015, 93: 822-830.

618 Millard, S.G., Molyneaux, T.C.K., Barnett, S.J., Gao, X. Dynamic enhancement of blast-  
619 resistant ultra high performance fibre-reinforced concrete under flexural and shear loading.  
620 *International Journal of Impact Engineering*, 2010, 37(4), 405-413.

621 Mechtcherine, V., Silva, F.A., Butler, M., Zhu, D., Mobasher, B., Gao, S.L., Mader, E.  
622 Behaviour of strain-hardening cement-based composites under high strain rates. *Journal of  
623 Advanced Concrete Technology*, 2011, 9(1), 51-62.

624 Naaman, A.E., Reinhardt, H.W. High performance fibre reinforced cement composites 2  
625 (HPRCC2). Proceedings of the 2<sup>nd</sup> International Workshop 'High Performance Fibre  
626 Reinforced Cement Composites', Ann Arbor, USA, 1995.

627 Odeh, A.A. Modelling and Simulation of bogie impacts on concrete bridge rails using LS-  
628 DYNA. 10<sup>th</sup> International LS-DYNA Users Conference, Dearborn, Michigan, USA, 2008.

629 Park, S.H., Kim, D.J., Ryu, G.S., Koh, K.T. Tensile behaviour of ultra high performance hybrid  
630 fiber reinforced concrete. *Cement and Concrete Composites*, 2012, 34(2), 172-184.

631 Schleyer, G.K., Underwood, N.J., Do, H.M., Paik, J.K., Kim, B.J. On pulse pressure loading of  
632 plates with holes, *Central European Journal of Engineering*, 2012, 2(4), 496-508.

633 Schleyer, G.K., Barnett, S.J., Millard, S.G., Wight, G. Modelling the response of UHPFRC  
634 panels to explosive loading. 11<sup>th</sup> International Conference on Structures under Shock and  
635 Impact, Tallinn, Estonia, 2010.

636 Tanapornraweekit, G., Haritos, N, Mendis, P., Ngo, T. Modelling of a reinforced concrete  
637 panel subjected to blast load by explicit non-linear FE code. Proceedings of Earthquake  
638 Engineering in Australia Conference 2007, Wollongong, NSW, Australia, 2007.

639 Tu, Z.G., Lu, Y. Evaluation of typical concrete material models used in hydrocodes for high  
640 dynamic response simulations. *International Journal of Impact Engineering*, 2009, 36(1),  
641 132-146.

642 Yi, N.H., Kim, J.H.J., Han, T.S., Cho, Y.G., Lee, J.H. Blast-resistant characteristics of ultra-high  
643 strength concrete and reactive powder concrete. *Construction and Building Materials*, 2012,  
644 28(1), 694-707.